



Crest Factor Reduction for Down-link LTE by Transmitting Phase Shifted Resource Blocks



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Goal

- Crest factor reduce (CFR) the LTE down-link waveform.
 - OFDM.
 - High PAPR (peak to average power ratio).
- Modify Partial Transmit Sequence (PTS) approach to CFR
 - Exploit the structure of the LTE down-link waveform.
 - Improve computational efficiency.



Outline

- Brief summary of CFR approaches.
- Review LTE down-link waveform.
 - Modulation
 - Demodulation
- Proposed method (exploiting the down-link LTE structure).
 - Apply phase shifts to resource blocks during modulation.
 - Equalize resource blocks independently during demodulation.
- Proposed CFR algorithm.
 - Apply small phase shifts to many resource blocks instead of π radians shifts to a few.
 - Descent-based optimization instead of an exhaustive search.

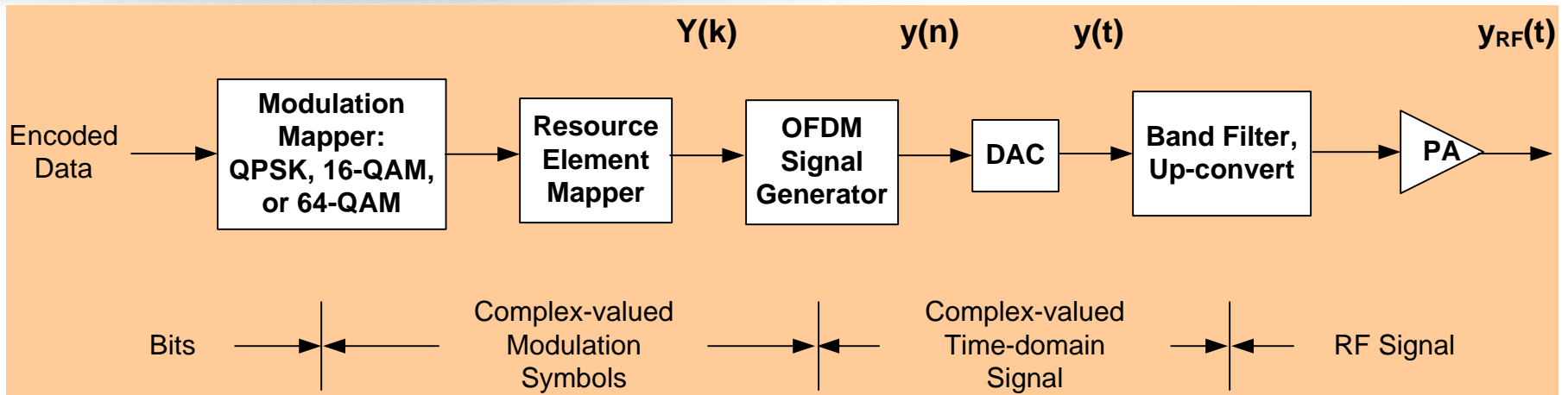


Summary of CFR Approaches

- **Clip and filter**
 - Find peaks above a threshold and create a clipped error waveform.
 - Bandlimit clipped error and subtract it from original waveform.
 - Increases EVM.
- **Tone reservation**
 - Transmit sequences on unused sub-carriers to reduce peaks.
 - Increases Tx power, reduces throughput.
- **Constellation extension**
 - Map opposing constellation points to one symbol: $c_{IQ} = -c_{IQ}$.
 - Reduces throughput (QPSK $\frac{1}{2}$, 16QAM $\frac{3}{4}$, 64QAM $\frac{5}{6}$).
- **Partial transmit sequence (PTS), selective mapping (SLM)**
 - Phase shift blocks of sub-carriers to reduce peaks.
 - Phase shift vector must be transmitted to the receiver.



LTE Down-link Waveform



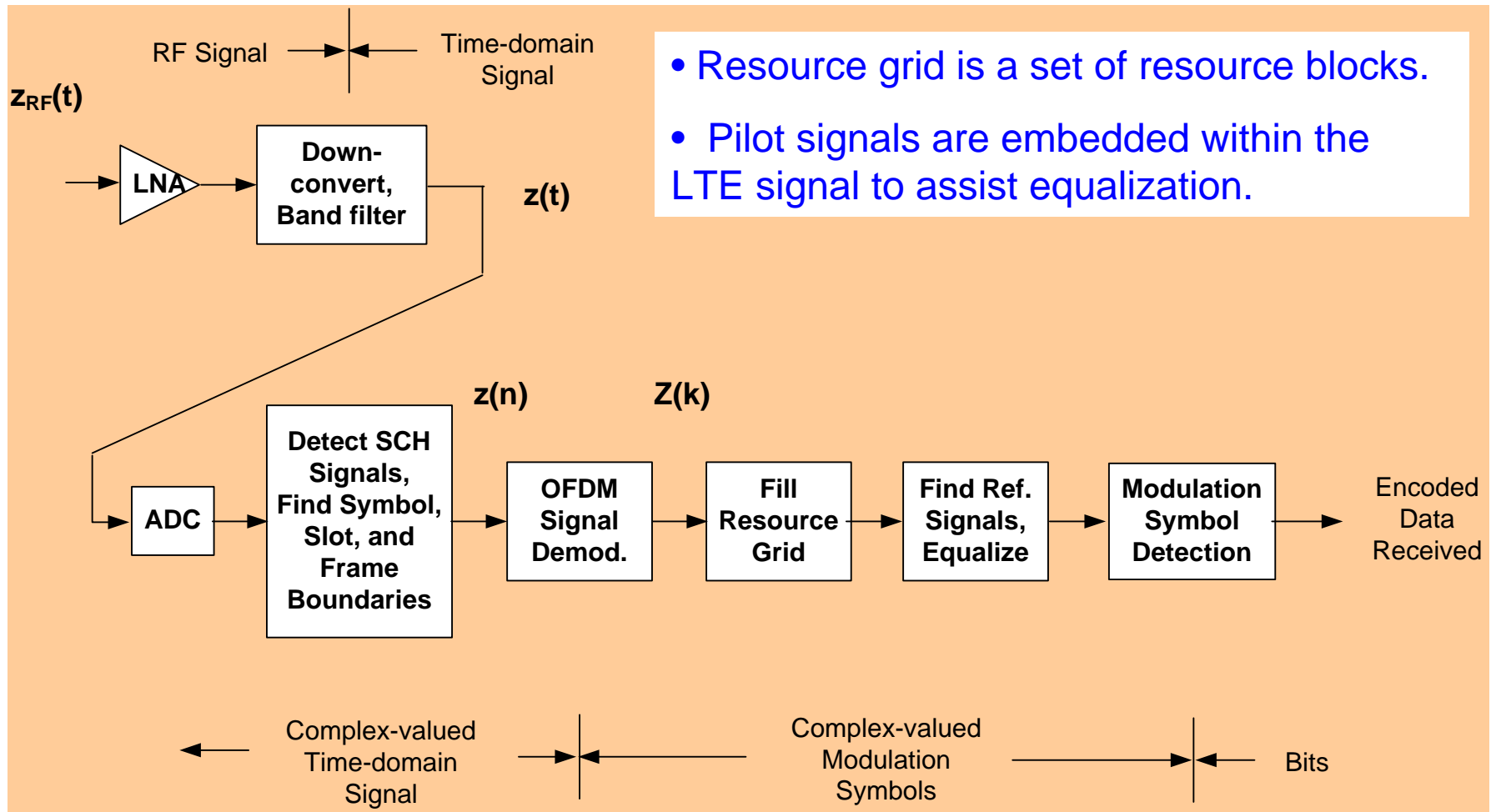
- **Resource element**

- time-frequency point holding modulated data.
- QPSK, 16QAM, 64QAM modulation.

- **Resource block**

- Group of resource elements contiguous in time and frequency.
- Minimum allocation unit for data transmission.

LTE Down-link Receiver

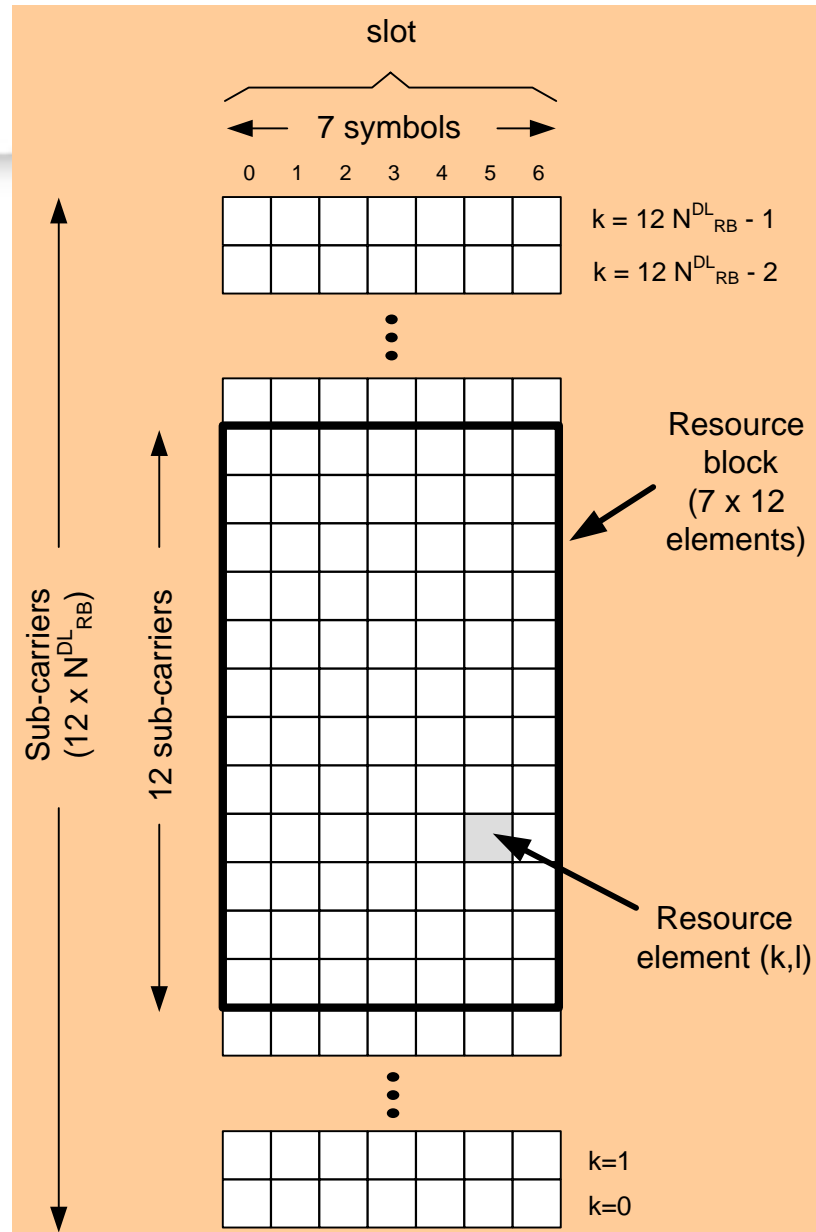


- Resource grid is a set of resource blocks.
- Pilot signals are embedded within the LTE signal to assist equalization.



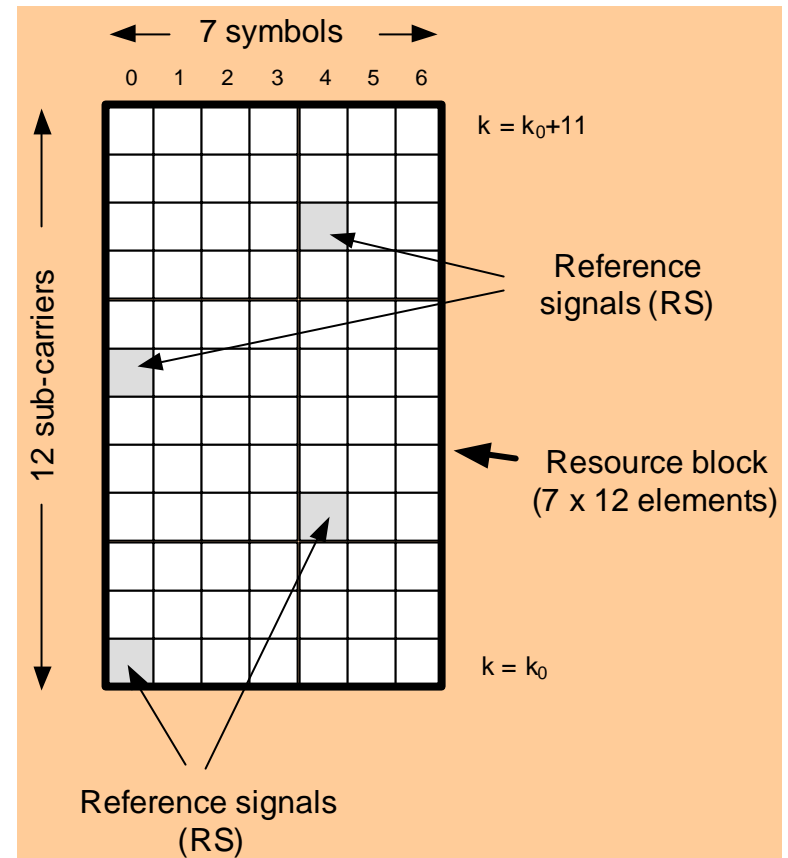
Resource Grids, Blocks, and Elements

- **Resource Grid**
 - Several resource blocks (RB's).
 - Number of RB's adjusted to cover available BW.
- **Resource Block (RB)**
 - 7 by 12 elements.
 - Transmissions are allocated in discrete RB's.
- **Resource element**
 - one symbol width in time
 - one 15 kHz sub-carrier in frequency.

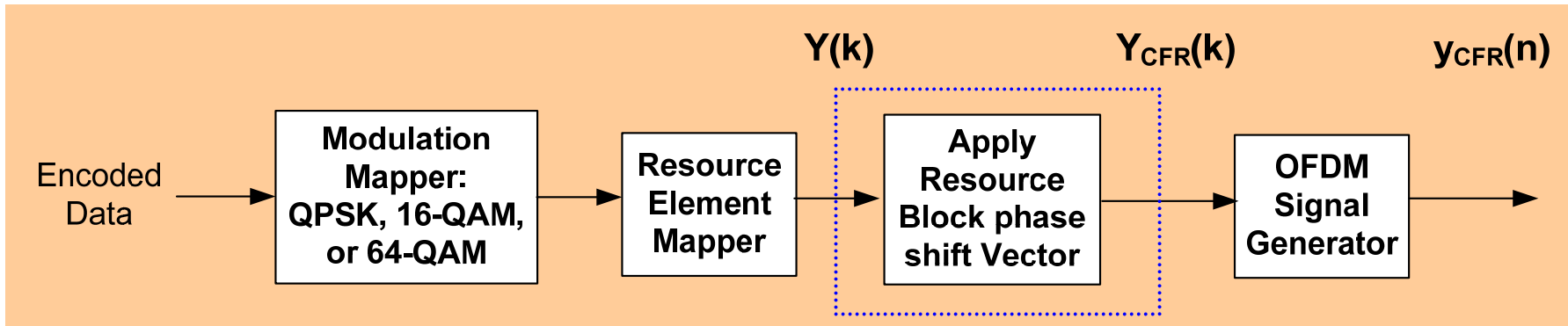


LTE Reference Signal (RS)

- Reference signals
 - Pilot signals.
 - Occupy four elements per resource block for the single antenna port case.
- Used by the receiver
 - Equalize channel propagation.
- Proposed approach
 - Use the 4 available reference signals to equalize each resource block independently.
 - A phase shift applied to a RB is removed during demodulation.



LTE Down-link CFR



- Phase shift vector

- Phase shift resource blocks to reduce peaks..

Partial Transmit Sequence CFR for OFDM

- Original OFDM signal

$$y(t) = \sum Y_k \exp[j k \Delta\omega t]$$

- CFR'ed signal

$$y_{\text{CFR}}(t) = \sum Y_k \exp[j (k \Delta\omega t + \theta_k)]$$

- Select phase shift vector θ_k to reduce peaks.
 - Phase shift groups of subcarriers.
 - Resource blocks for LTE case.



Baseline Approach for PTS

$$y_{\text{CFR}}(t) = \sum Y_k \exp[j (k \Delta\omega t + \theta_k)]$$

- Restrict allowable phase shifts to reduce search space.
 - $\theta_k = [0, \pi]$ radians.
- Neighborhood gradient search (NGS). [Han & Lee]
 - Phase shift one resource block by π radians.
 - Test if $\max\{ |y_{\text{CFR}}(t)| \} > \max\{ |y(t)| \}$
 - Apply phase shift to next RB and retest (for all remaining RB's).
 - Retain best $y_{\text{CFR}}(t)$.
 - Make $y(t) = y_{\text{CFR}}(t)$, and repeat to introduce additional phase shifts.
- Sub-optimal search.
 - Number of FFT / IFFT = (num of RB's) x (num of phase shifts).



Small Phase Angle CFR for OFDM

$$y_{\text{CFR}}(t) = \sum Y_k \exp[j (k \Delta\omega t + \theta_k)]$$

- Clipped peaks signal

$$y_{\text{peaks}}(t) = y(t) - y_{\text{CFR}}(t)$$

- For small angles $|\theta_k|$

$$\sum Y_k \theta_k \exp[j k \Delta\omega t] \approx j y_{\text{peaks}}(t)$$

- FFT of desired $j y_{\text{peaks}}(t)$ provides phase shift vector θ_k .
- Not practical to phase shift each resource element separately.
- Modify approach by phase shifting resource blocks.



Proposed Approach (one iteration)

- Compute peak signal (exceeds threshold λ)

$$y_{peaks}(n) = \begin{cases} y(n) - \lambda \cdot \frac{y(n)}{|y(n)|} & \text{for } |y(n)| > \lambda \\ 0 & \text{otherwise} \end{cases}$$

- Cross-correlate $Y = \text{FFT}\{y\}$ and $Y_{peaks} = \text{FFT}\{y_{peaks}\}$
 - for each resource block b

$$C_{RB}(b) = \sum_k \sum_l Y(k,l) Y_{peaks}(k,l)^*$$

- Compute phase shift

$$\theta(b) = \begin{cases} |\Delta\theta| \cdot \text{sgn}(\text{Im}\{C_{RB}(b)\}) & \text{for } \text{Re}\{C_{RB}(b)\} > 0 \\ 0 & \text{otherwise} \end{cases}$$



Complexity Comparison

- Number of FFT / IFFT calculation made (N_{FFT}).
- Proposed approach (small phase shifts)

$$N_{\text{FFT}} = 2 N_{\text{iter}} + 1$$

– Number of iterations $N_{\text{iter}} = 3$, typically. ($N_{\text{FFT}} = 7$).

- Baseline approach (NGS)

$$N_{\text{FFT}} = N_{\text{RB}} N_{\text{iter}}$$

– Number of resource blocks $N_{\text{RB}} = 50$ for 10 MHz BW.

– N_{iter} is also the number of π phase shifts applied (4.2 on average).

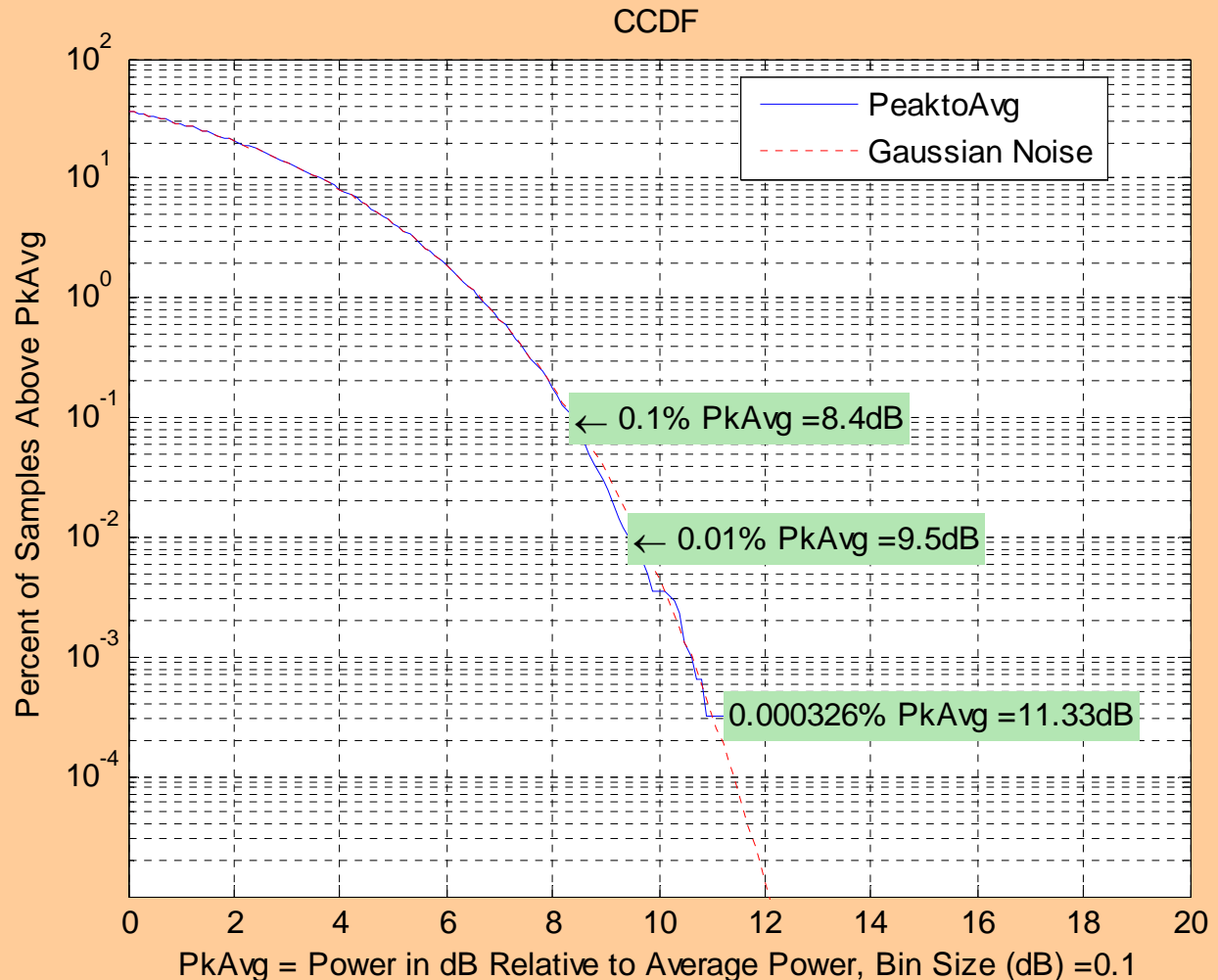
– $N_{\text{FFT}} = 210$.

- Proposed approach is better.



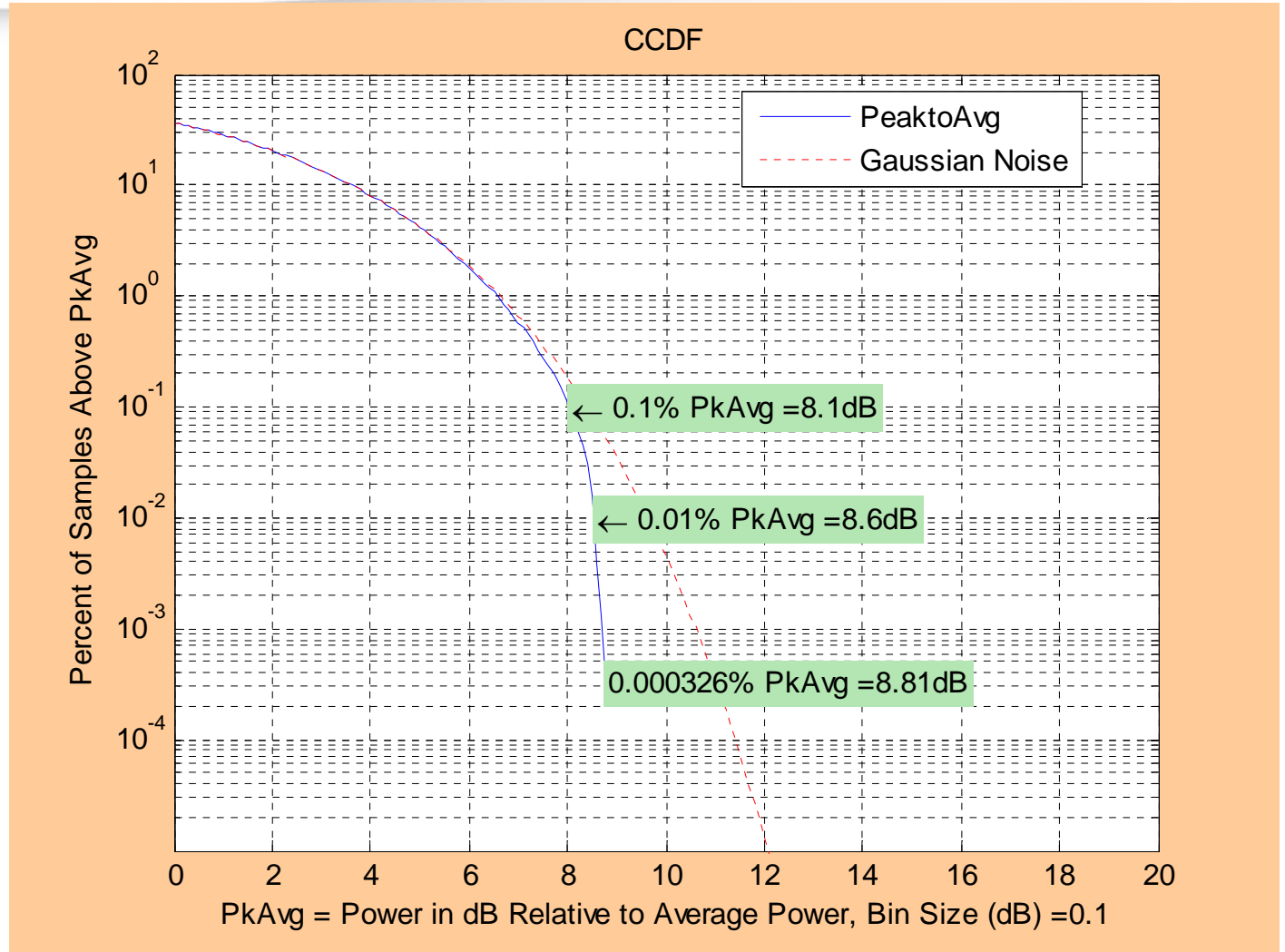
Results: LTE waveform, No CFR

- CCDF of LTE is similar to that of Gaussian noise.
- PAPR = 11.3 dB.



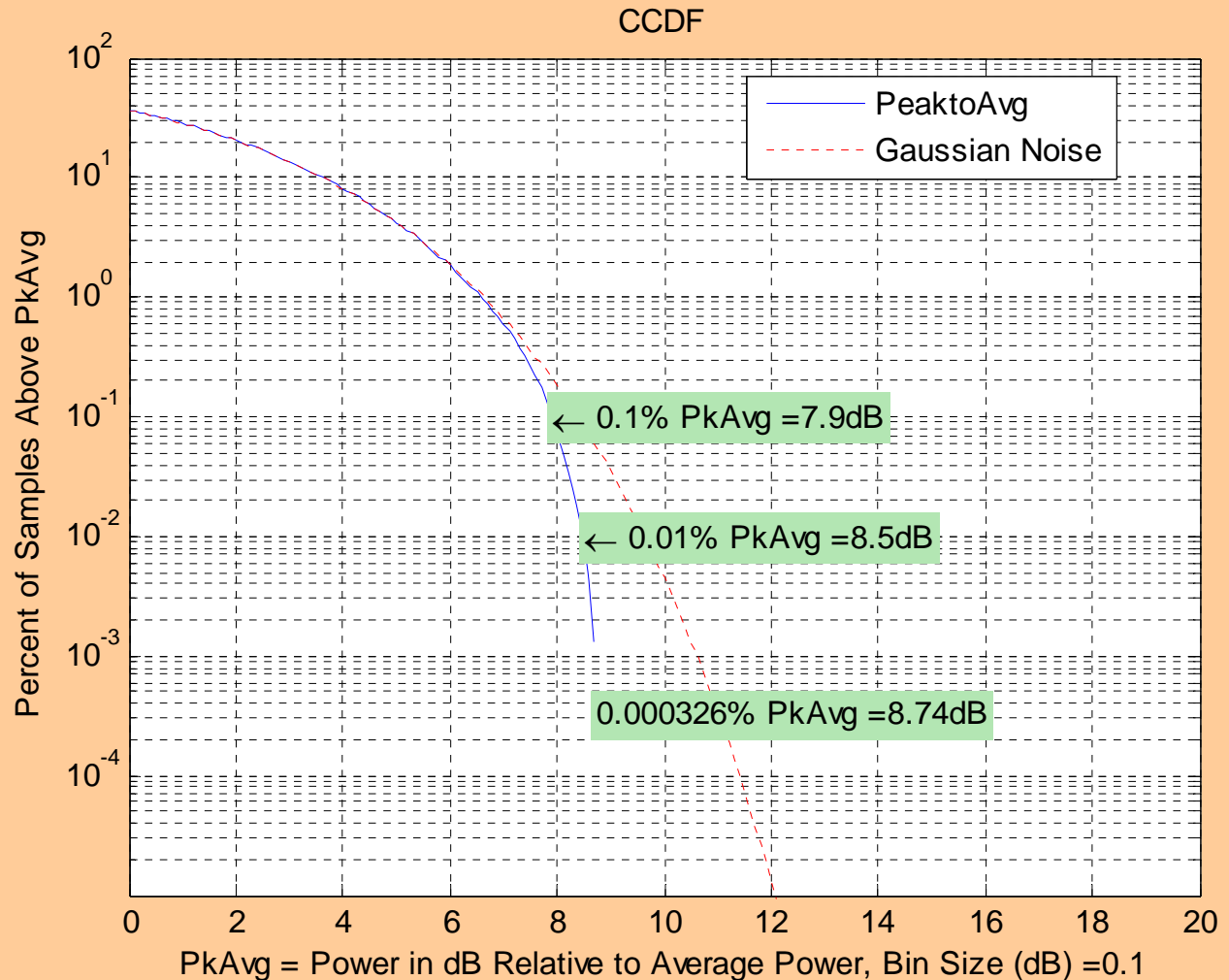
Results: Baseline CFR (NGS)

- NGS CFR reduces the PAPR by 2.5 dB.
- PAPR = 8.8 dB.
EVM = 0.
- Compare clipping to 8.8 dB
3.5% EVM



Results: Proposed Approach (small $|\theta|$)

- Proposed CFR reduces PAPR by 2.6 dB.
- PAPR = 8.7 dB.
- Slightly better than baseline.



Conclusion

- CFR method for LTE.
 - Modification of the partial transmit sequence (PTS) approach.
 - Apply phase shifts to resource blocks during modulation.
 - Equalize resource blocks independently during demodulation.
- Computationally efficient search algorithm.
 - Apply small phase shifts to many resource blocks instead of π radians shifts to a few.
 - Descent-based optimization instead of an exhaustive search.

