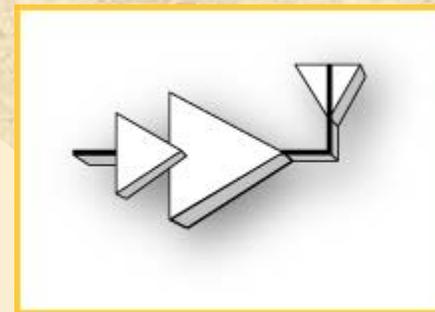




**2009 Radio and Wireless Week
Power Amplifier Symposium**



**HIGH-EFFICIENCY
RF AND MICROWAVE POWER AMPLIFIERS:
HISTORICAL ASPECT AND MODERN TRENDS**

Dr. Andrei Grebennikov

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**HIGH-EFFICIENCY
RF AND MICROWAVE POWER AMPLIFIERS:
HISTORICAL ASPECT AND MODERN TRENDS**

**I. POLYHARMONIC CLASS F AND INVERSE CLASS F
POWER AMPLIFIERS**

II. SWITCHED-MODE CLASS E POWER AMPLIFIERS

III. SWITCHED-MODE CLASS FE POWER AMPLIFIERS

POLYHARMONIC CLASS F AND INVERSE CLASS F POWER AMPLIFIERS

1. Class F: biharmonic and polyharmonic operation modes
2. Class F with quarterwave transmission line
3. Class F : load networks with lumped elements and transmission lines
4. Class F: LDMOSFET power amplifier design examples
5. Inverse Class F: biharmonic and idealized operation modes
6. Inverse Class F: load networks with lumped elements and transmission lines
7. Inverse Class F: LDMOSFET power amplifier design examples
8. Practical high-efficiency Class F power amplifiers

1. Class F: biharmonic and polyharmonic operation modes

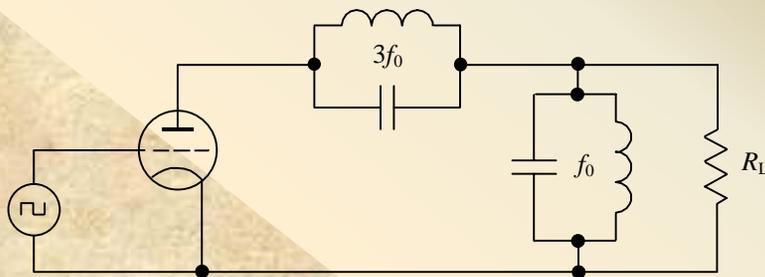
Fourier series for:

rectangular voltage waveform

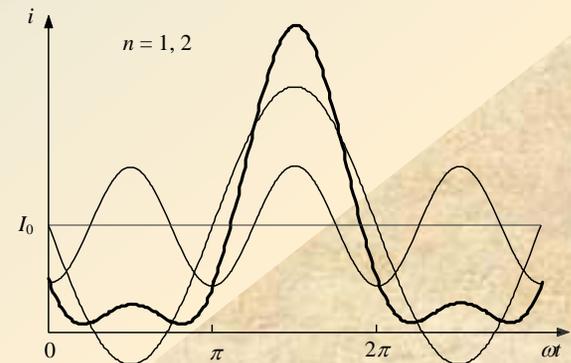
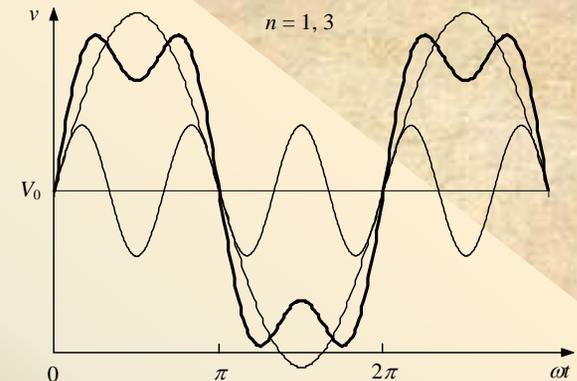
$$\frac{v(\omega t)}{V_0} = 1 + \frac{4}{\pi} \sin \omega t + \frac{4}{3\pi} \sin 3\omega t + \frac{4}{\pi} \sum_{n=5,7,\dots}^N \frac{\sin n\omega t}{n}$$

half-sinusoidal current waveform

$$\frac{i(\omega t)}{I_0} = 1 - \frac{\pi}{2} \sin \omega t - \frac{2}{3} \cos 2\omega t - 2 \sum_{n=4,6,\dots}^N \frac{\cos n\omega t}{n^2 - 1}$$

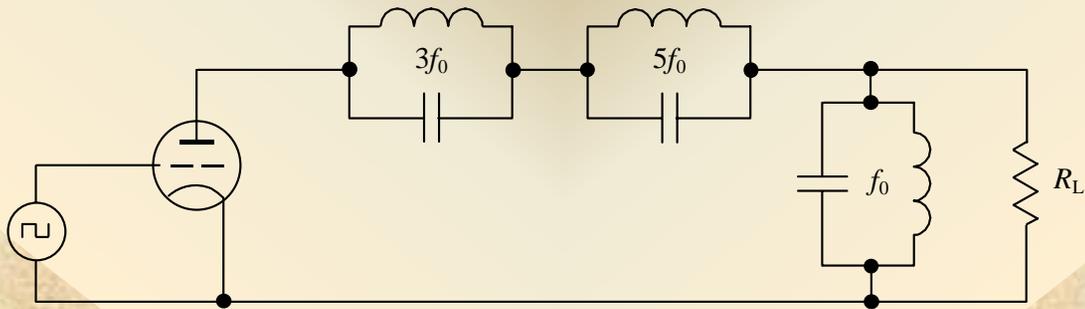
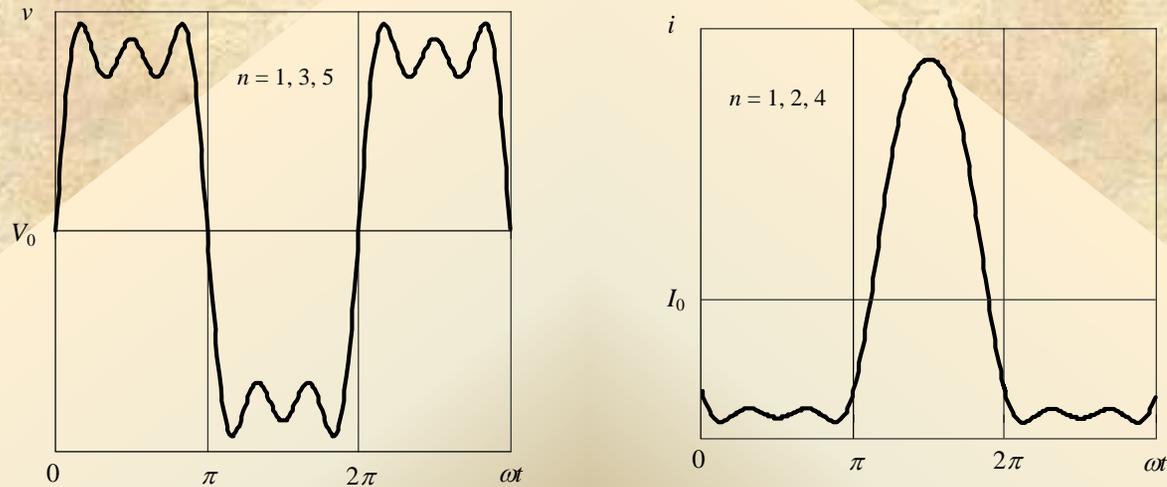


Third-harmonic peaking



D. C. Prince, "Vacuum Tubes as Power Oscillators, Part III,"
Proc. IRE, vol. 11, pp. 527-550, Sept. 1923

1. Class F: biharmonic and polyharmonic operation modes

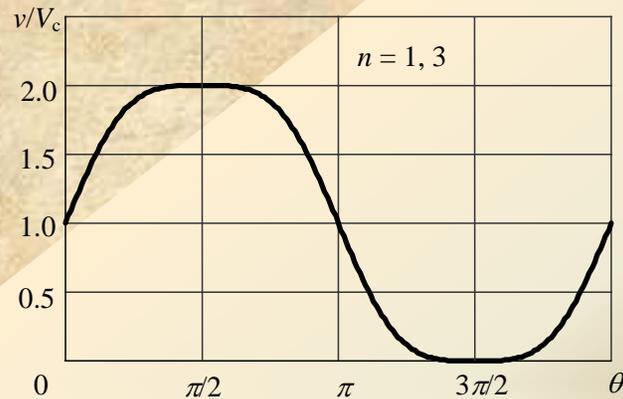


H. J. Round, "Wireless Telegraph and Telephone Transmission,"
U.S. Patent 1,564,627, Dec. 1925

1. Class F: biharmonic and polyharmonic operation modes

For maximally flat waveforms

collector voltage

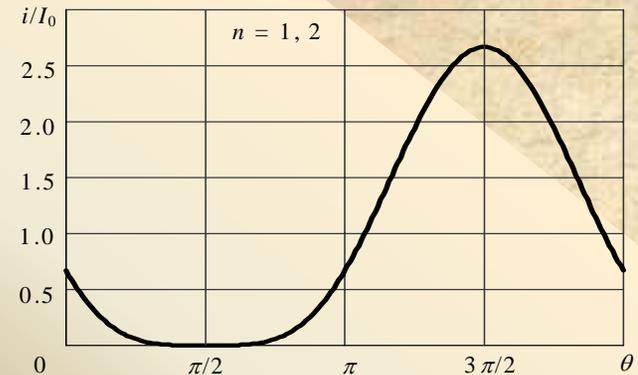


$$V_1 = \frac{9}{8} V_{cc}$$

$$V_3 = \frac{1}{8} V_{cc}$$

optimum values

collector current



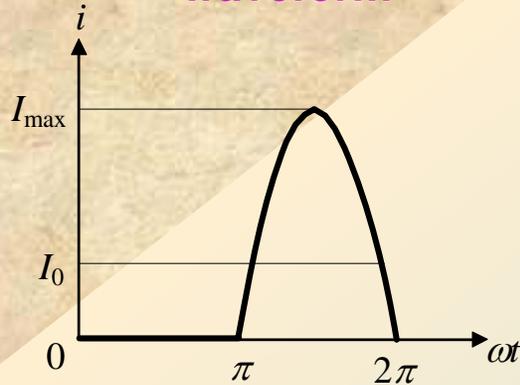
$$I_1 = \frac{4}{3} I_0$$

$$I_2 = \frac{1}{3} I_0$$

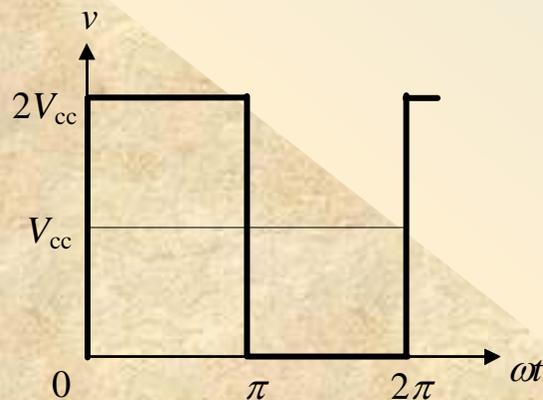
Current harmonic components	Voltage harmonic components				
	1	1, 3	1, 3, 5	1, 3, 5, 7	1, 3, 5, ..., ∞
1	$1/2 = 0.500$	$9/16 = 0.563$	$75/128 = 0.586$	$1225/2048 = 0.598$	$2/\pi = 0.637$
1, 2	$2/3 = 0.667$	$3/4 = 0.750$	$25/32 = 0.781$	$1225/1536 = 0.798$	$8/3\pi = 0.849$
1, 2, 4	$32/45 = 0.711$	$4/5 = 0.800$	$5/6 = 0.833$	$245/288 = 0.851$	$128/45\pi = 0.905$
1, 2, 4, 6	$128/175 = 0.731$	$144/175 = 0.823$	$6/7 = 0.857$	$7/8 = 0.875$	$512/175\pi = 0.931$
1, 2, 4, ..., ∞	$\pi/4 = 0.785$	$9\pi/32 = 0.884$	$75\pi/256 = 0.920$	$1225\pi/4096 = 0.940$	$1 = 1.000$

1. Class F: idealized operation mode

Ideal current waveform



Ideal voltage waveform



$$I_1 = \frac{I_{\max}}{2} \quad \text{- fundamental current component}$$

$$V_1 = \frac{4V_{cc}}{\pi} \quad \text{- fundamental voltage component}$$

$$I_0 = \frac{I_{\max}}{\pi} \quad \text{- dc current component}$$

$$P_1 = \frac{V_{cc} I_{\max}}{\pi} \quad \text{- fundamental output power}$$

$$P_0 = V_{cc} I_0 \quad \text{- dc supply power}$$

$$\eta = \frac{P_1}{P_0} = 100\% \quad \text{- collector/drain efficiency}$$

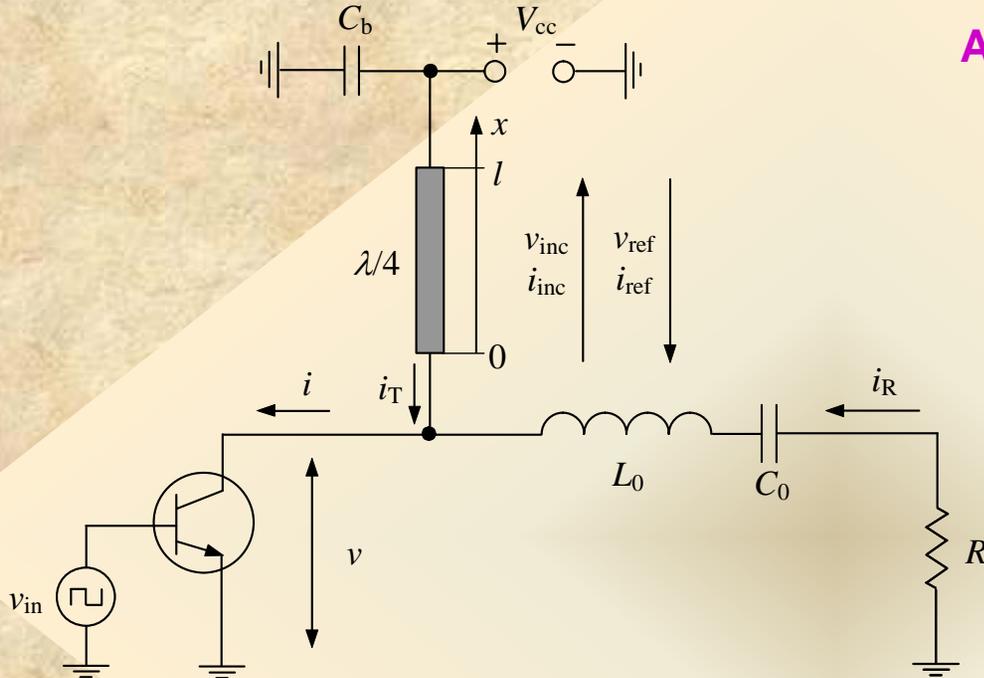
Harmonic impedance conditions:

$$Z_1 = R_1 = \frac{8}{\pi} \frac{V_{cc}}{I_{\max}} = \frac{8}{\pi^2} \frac{V_{cc}}{I_0}$$

$$Z_n = 0 \quad \text{for even } n$$

$$Z_n = \infty \quad \text{for odd } n$$

2. Class F with quarterwave transmission line



Assumptions for transistor:

- *ideal switch:*
no parasitic elements
- *half period is on,*
half period is off:
50% duty cycle

Assumptions for load:

- *sinusoidal current:*
ideal L_0C_0 -circuit
tuned to fundamental

$$i(\omega t) = I_R \sin \omega t \quad \text{- load current}$$

$$v(\omega t) = 2V_{cc} - v(\omega t + \pi)$$

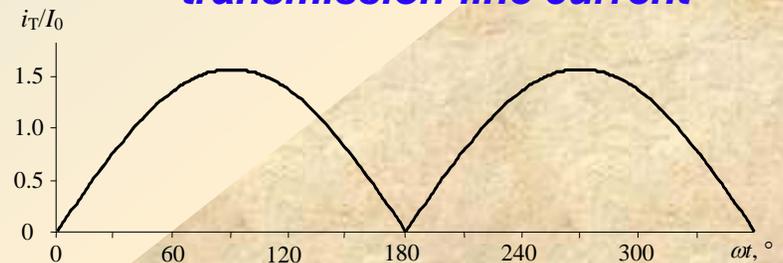
- collector voltage

$$i(\omega t) = I_R (\sin \omega t + |\sin \omega t|)$$

- collector current

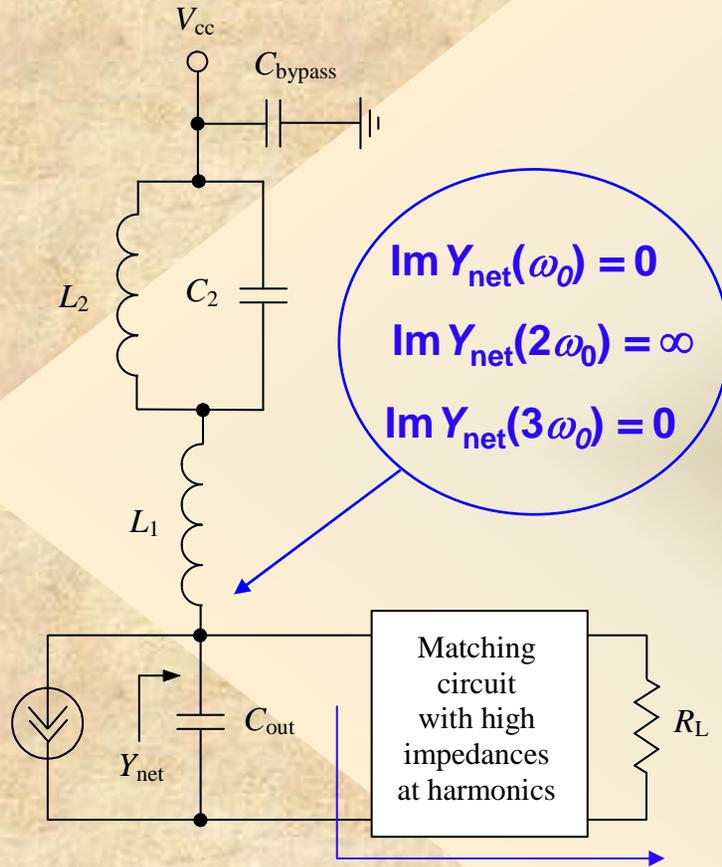
$$i_T(\omega t) = i_T(\omega t + \pi) = I_R |\sin \omega t|$$

- transmission-line current



3. Class F: second current and third voltage harmonic peaking

Load network



Circuit parameters

$$L_1 = \frac{1}{6\omega_0^2 C_{\text{out}}}, \quad L_2 = \frac{5}{3}L_1, \quad C_2 = \frac{12}{5}C_{\text{out}}$$

Output reactive admittance:

$$\text{Im}(Y_{\text{net}}) = \omega C_{\text{out}} - \frac{1 - \omega^2 L_2 C_2}{\omega L_1 (1 - \omega^2 L_2 C_2) + \omega L_2}$$

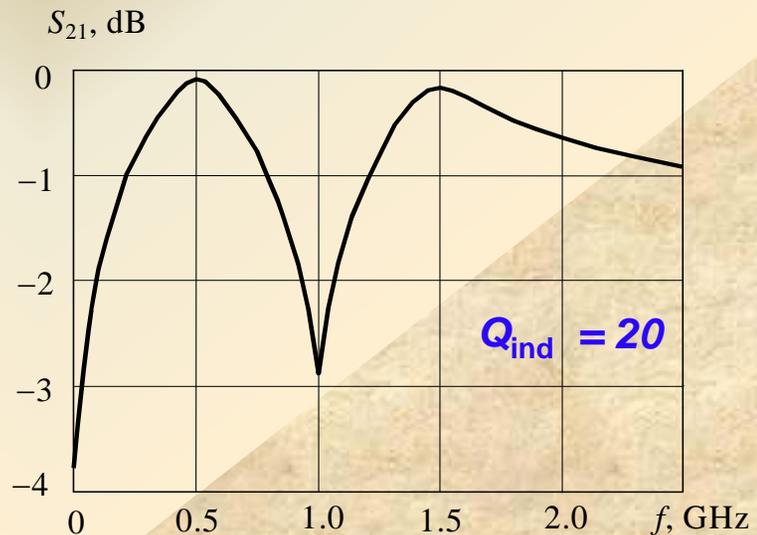
Three harmonic impedance conditions:

$$(1 - \omega_0^2 L_1 C_{\text{out}})(1 - \omega_0^2 L_2 C_2) - \omega_0^2 L_2 C_{\text{out}} = 0$$

$$L_1(1 - 4\omega_0^2 L_2 C_2) + L_2 = 0$$

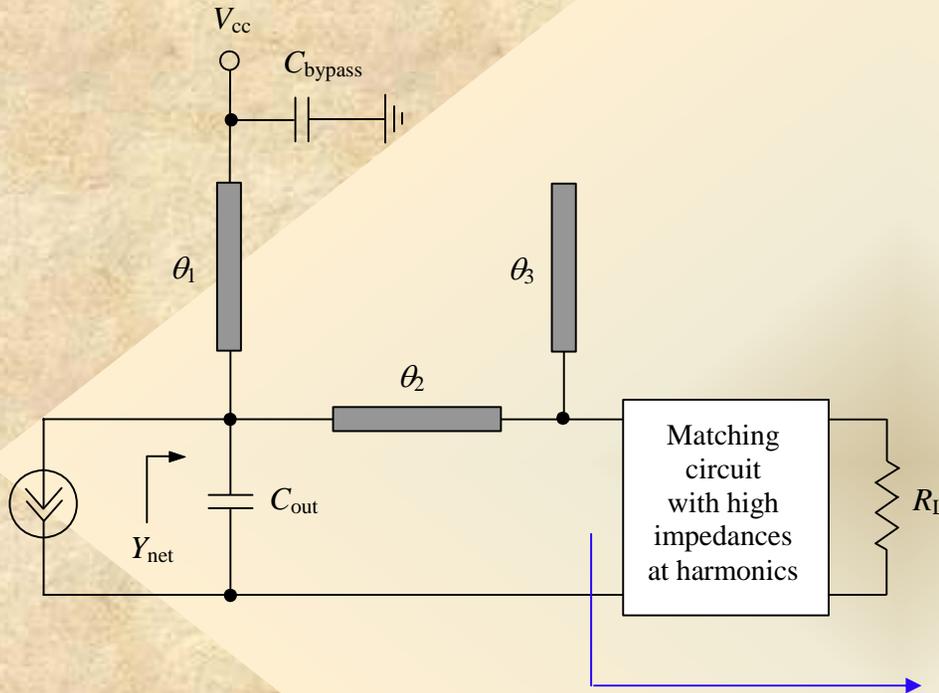
$$(1 - 9\omega_0^2 L_1 C_{\text{out}})(1 - 9\omega_0^2 L_2 C_2) - 9\omega_0^2 L_2 C_{\text{out}} = 0$$

S_{21} simulation ($f_0 = 500$ MHz)



3. Class F: even current and third voltage harmonic peaking

Load network



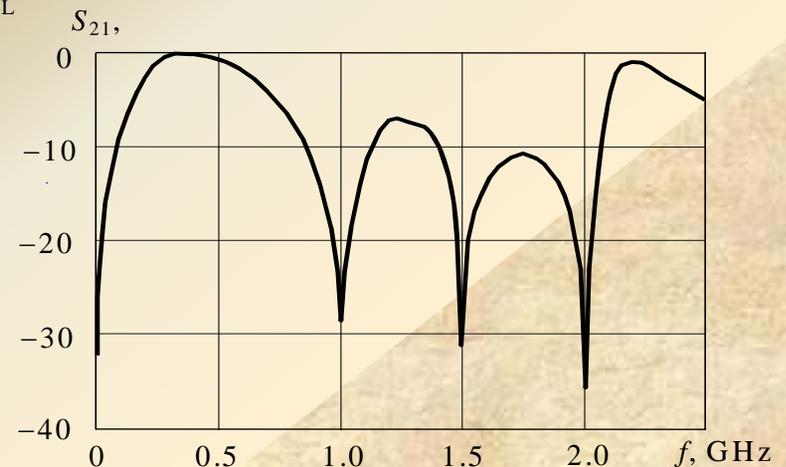
Harmonic impedance conditions at collector (drain):

$$\text{Im } Y_{\text{net}}(\omega_0) = 0$$

$$\text{Im } Y_{\text{net}}(2n\omega_0) = \infty$$

$$\text{Im } Y_{\text{net}}(3\omega_0) = 0$$

S_{21} simulation ($f_0 = 500$ MHz)



Circuit parameters:

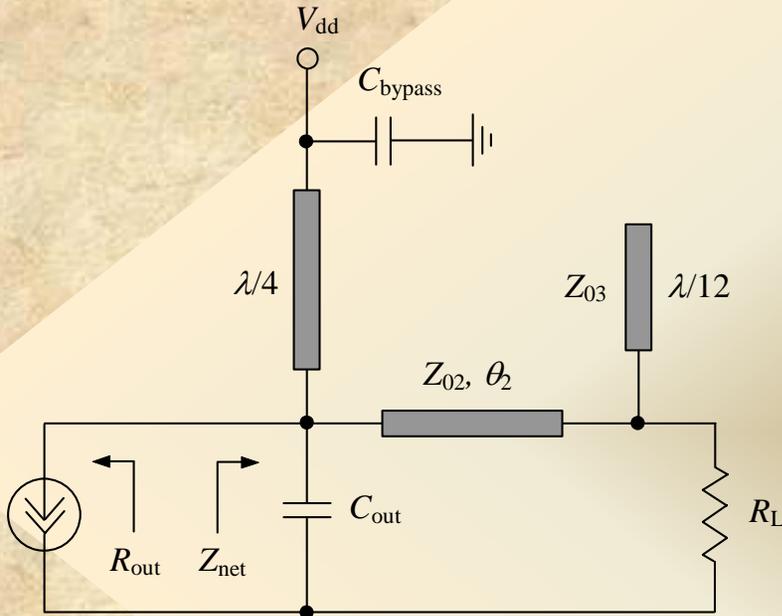
$$\theta_1 = \frac{\pi}{2}, \quad \theta_3 = \frac{\pi}{6}$$

$$\theta_2 = \frac{1}{3} \tan^{-1} \left(\frac{1}{3Z_0 \omega C_{\text{out}}} \right)$$

➤ **ideal transmission lines**

3. Class F: even current and third voltage harmonic peaking

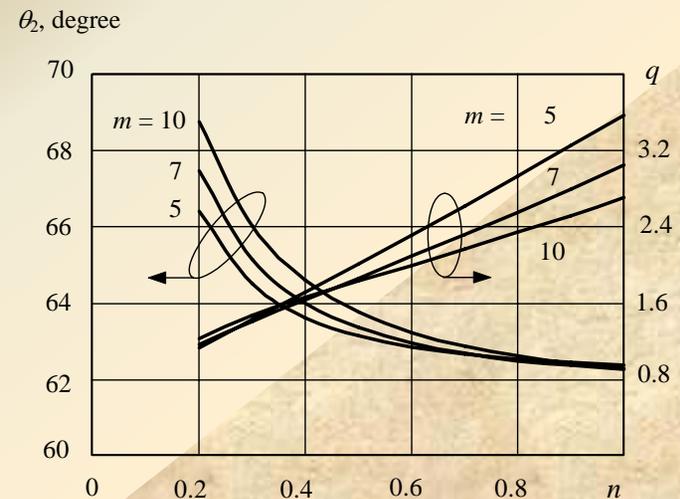
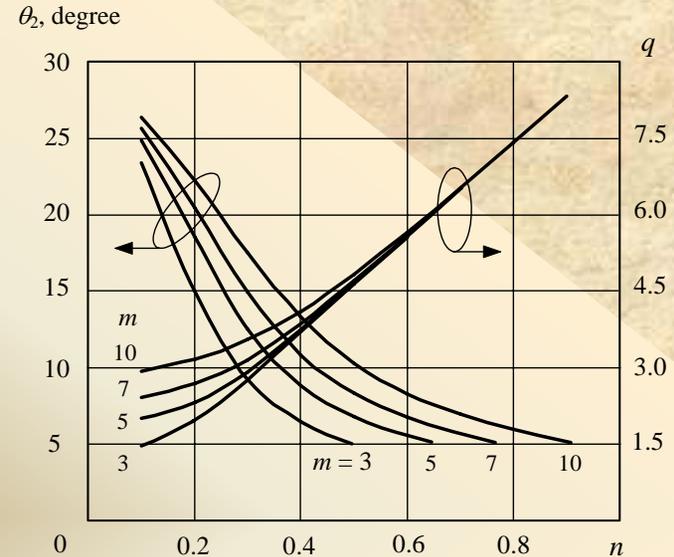
Load network with impedance matching



Normalized parameters:

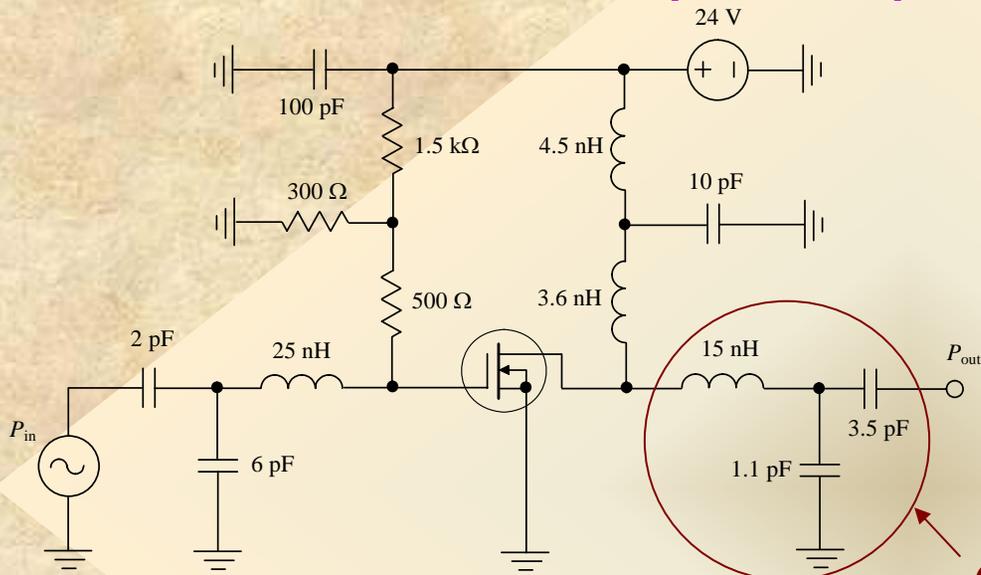
$$m = \frac{R_L}{R_{out}} \quad q = \frac{R_L}{Z_{03} \sqrt{3}}$$

$$n = \omega C_{out} Z_{02}$$

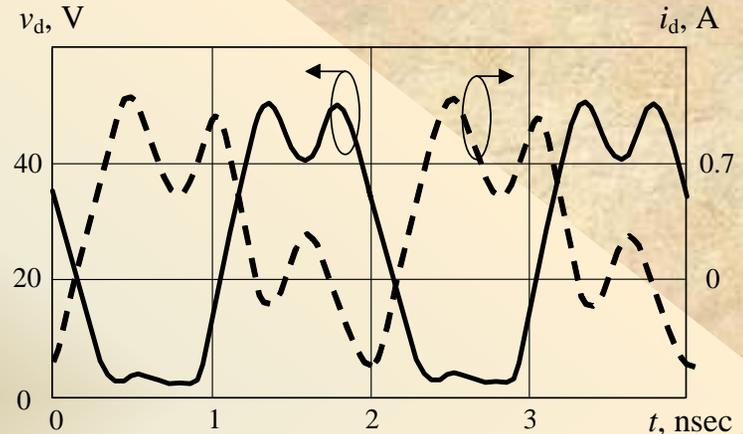


4. Class F: LDMOSFET power amplifier design example

500 MHz Class F power amplifier with lumped elements

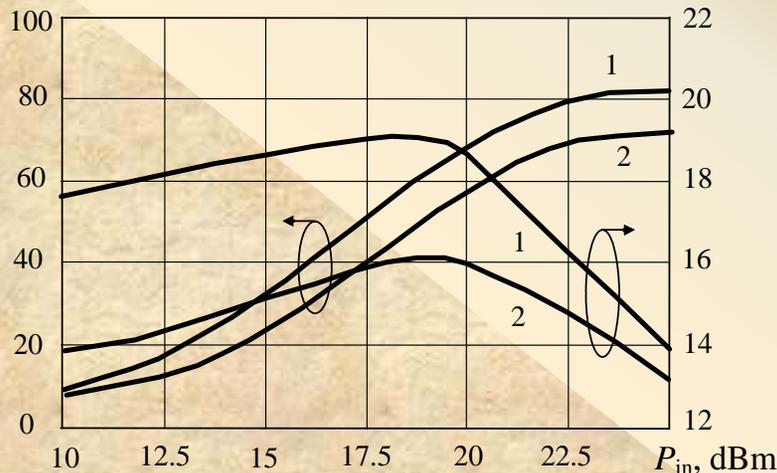


Drain voltage and current waveforms



efficiency, %

gain, dB



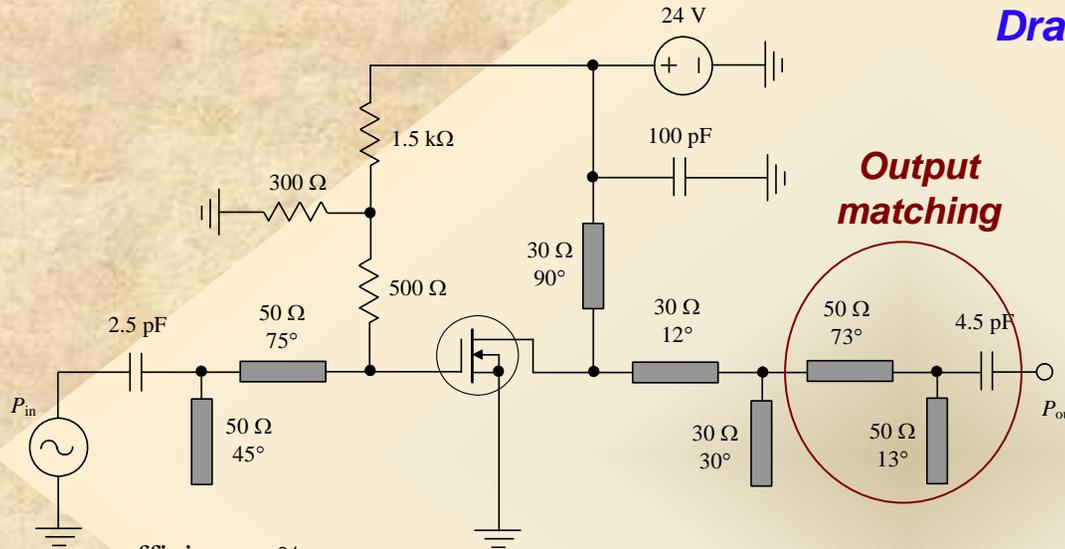
Output matching

LDMOSFET:
gate length 1.25 um
gate width 7x1.44 mm

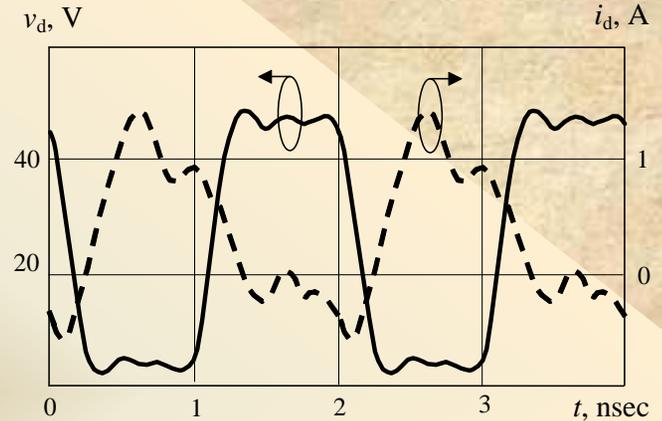
- inductance Q-factor = ∞
efficiency - 82%
linear power gain > 16 dB
- inductance Q-factor = 30
efficiency - 71%
linear power gain > 14 dB

4. Class F: LDMOSFET power amplifier design example

500 MHz Class F power amplifier with transmission lines

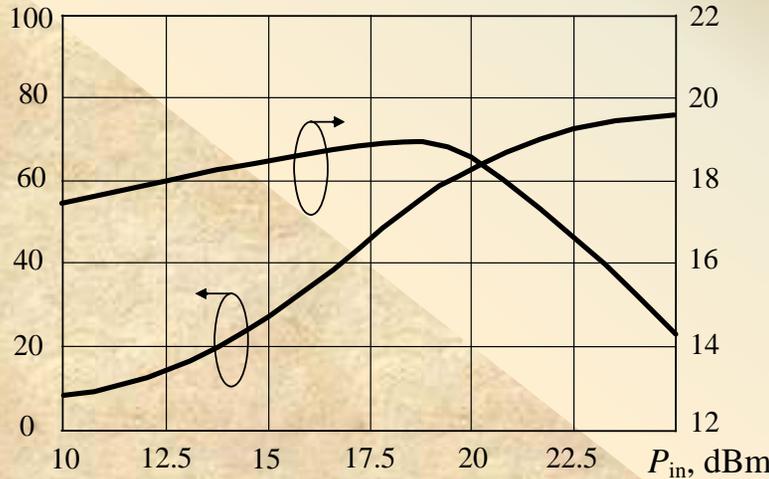


Drain voltage and current waveforms



efficiency, %

gain, dB



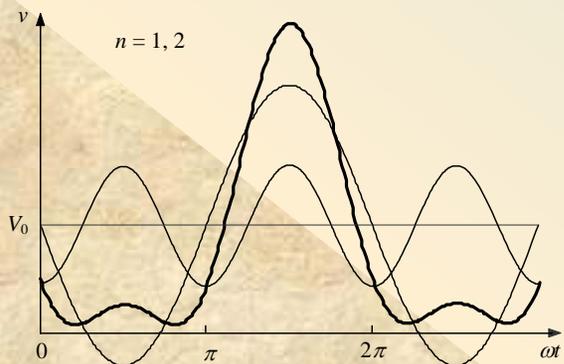
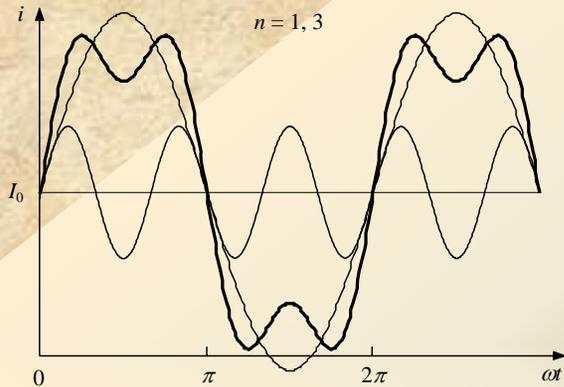
LDMOSFET:
gate length 1.25 μm
gate width 7x1.44 mm

- **T-matching circuit for output impedance transformation**
- **output power - 39 dBm (8 W)**
- **collector efficiency - 76%**
- **linear power gain > 16 dB**

5. Inverse Class F: biharmonic and idealized operation modes

Second-harmonic peaking

Inverse voltage and current waveforms



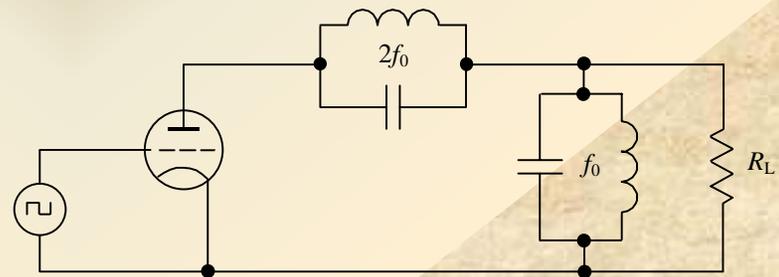
Fourier series for:

rectangular current waveform

$$\frac{i(\omega t)}{I_0} = 1 + \frac{4}{\pi} \sin \omega t + \frac{4}{3\pi} \sin 3\omega t + \frac{4}{\pi} \sum_{n=5,7,\dots}^N \frac{\sin n\omega t}{n}$$

half-sinusoidal voltage waveform

$$\frac{v(\omega t)}{V_0} = 1 - \frac{\pi}{2} \sin \omega t - \frac{2}{3} \cos 2\omega t - 2 \sum_{n=4,6,\dots}^N \frac{\cos n\omega t}{n^2 - 1}$$

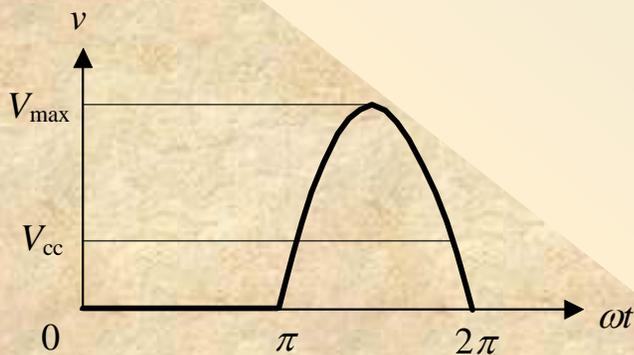
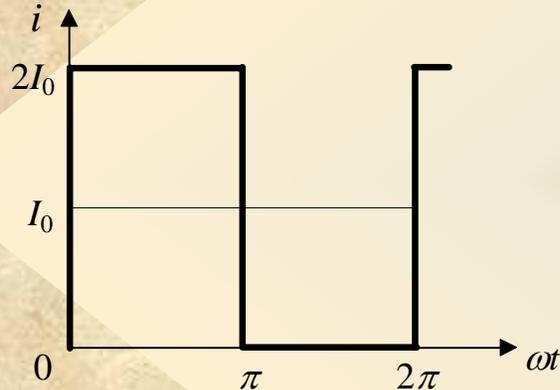


A. I. Kolesnikov, "A New Method to Improve Efficiency and to Increase Power of Transmitter (in Russian)," *Master Svyazi*, pp. 27-41, June 1940

5. Inverse Class F: idealized operation mode

Concept of inverse Class F mode was reintroduced for low voltage power amplifiers designed for monolithic applications (less collector current)

Dual to conventional Class F with mutually interchanged current and voltage waveforms



$$I_1 = \frac{4I_0}{\pi} \quad \text{- fundamental current}$$

$$V_1 = \frac{V_{\max}}{2} = \frac{\pi}{2} V_{cc} \quad \text{- fundamental voltage}$$

$$P_1 = \frac{V_{\max} I_0}{\pi} \quad \text{- fundamental output power}$$

$$P_0 = V_{cc} I_0 = \frac{V_{\max} I_0}{\pi} \quad \text{- dc output power}$$

$$\eta = \frac{P_1}{P_0} = 100\% \quad \text{- ideal collector/drain efficiency}$$

Harmonic impedance conditions:

$$Z_1 = R_1 = \frac{\pi}{8} \frac{V_{\max}}{I_0} = \frac{\pi^2}{8} \frac{V_{cc}}{I_0}$$

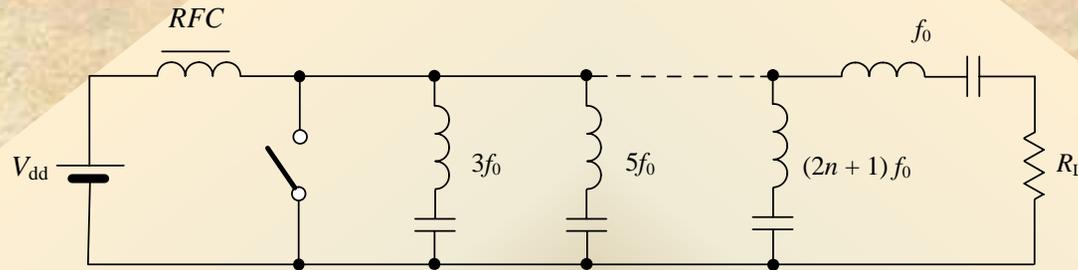
$$Z_n = 0 \quad \text{for odd } n$$

$$Z_n = \infty \quad \text{for even } n$$

5. Inverse Class F with quarterwave transmission line

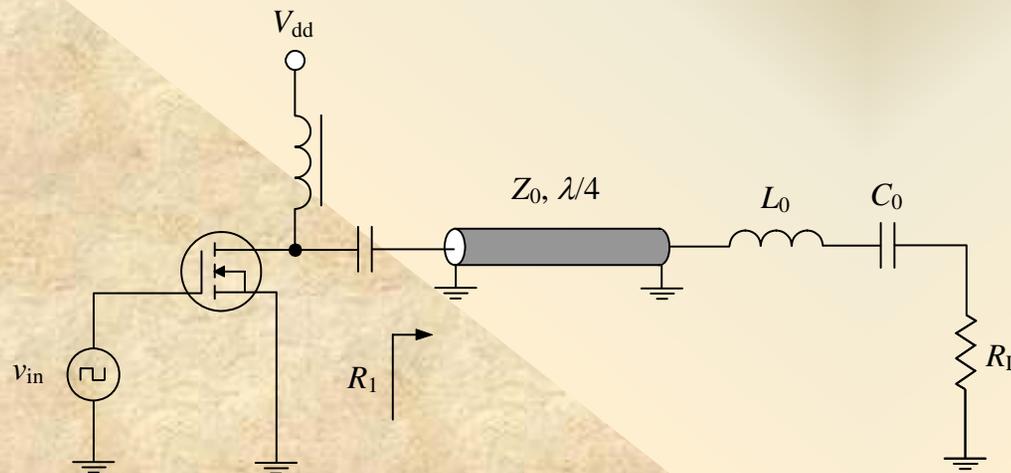
➤ *device is driven to operate as switch*

➤ *zero impedances at odd harmonic components*



➤ *quarterwave transmission line as infinite set of series resonant circuits*

➤ *sinusoidal current: shunt L_0C_0 -circuit tuned to fundamental*



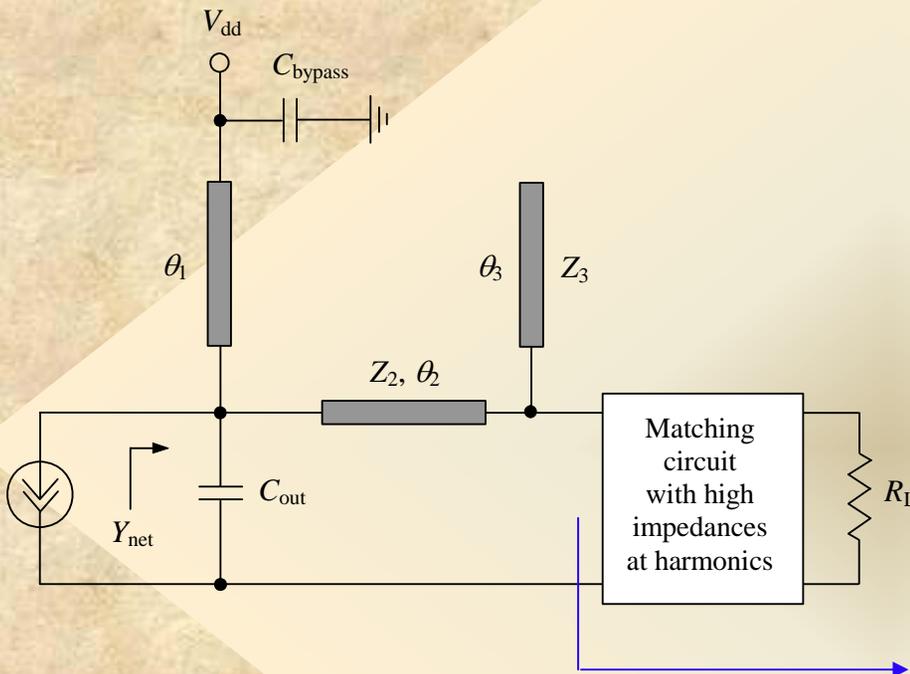
➤ *quarterwave transmission line as impedance transformer*

$$R_1 = \frac{Z_0^2}{R_L}$$

6. Inverse Class F: second current and third voltage harmonic peaking

Load network

Harmonic impedance conditions at collector (drain):

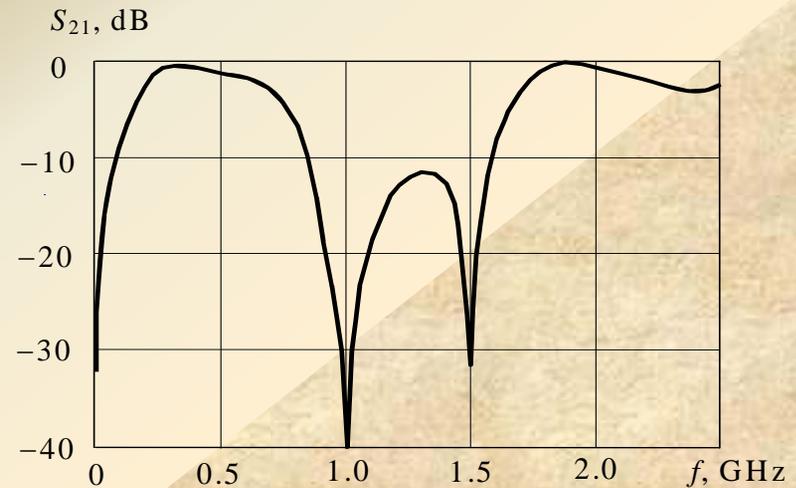


$$\text{Im } Y_{\text{net}}(\omega_0) = 0$$

$$\text{Im } Y_{\text{net}}(2\omega_0) = 0$$

$$\text{Im } Y_{\text{net}}(3\omega_0) = \infty$$

S_{21} simulation ($f_0 = 500$ MHz)



Circuit parameters:

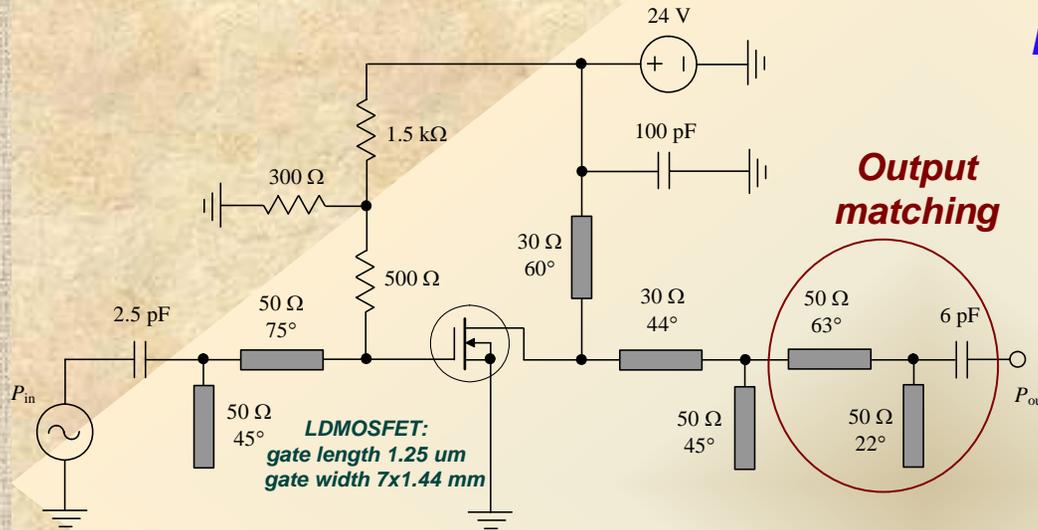
$$\theta_1 = \frac{\pi}{3}, \quad \theta_3 = \frac{\pi}{4}$$

$$\theta_2 = \frac{1}{2} \tan^{-1} \left[\left(2Z_0 \omega C_{\text{out}} + \frac{1}{\sqrt{3}} \right)^{-1} \right]$$

➤ **ideal transmission lines**

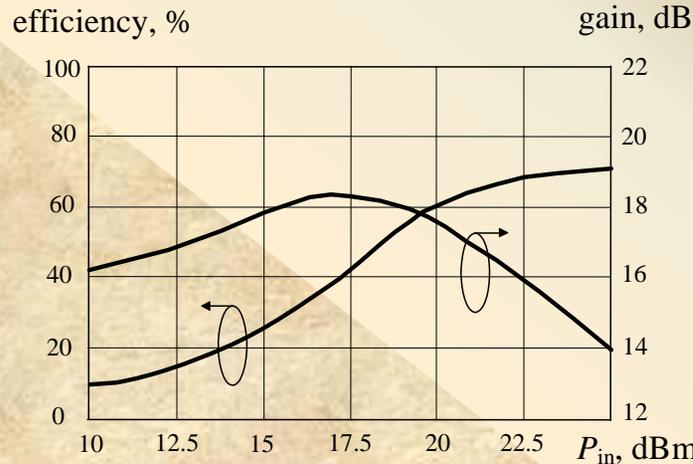
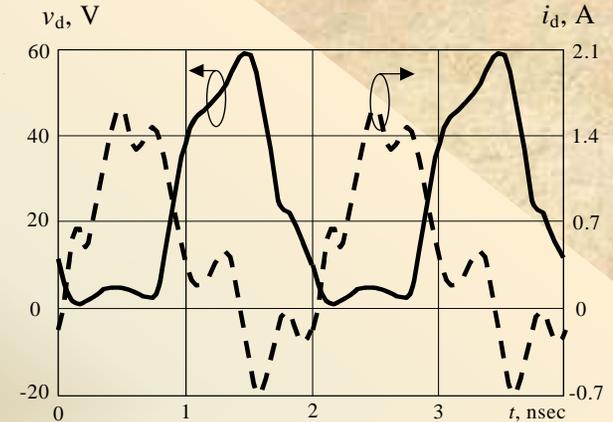
7. Inverse Class F: LDMOSFET power amplifier design example

500 MHz inverse Class F power amplifier with transmission lines

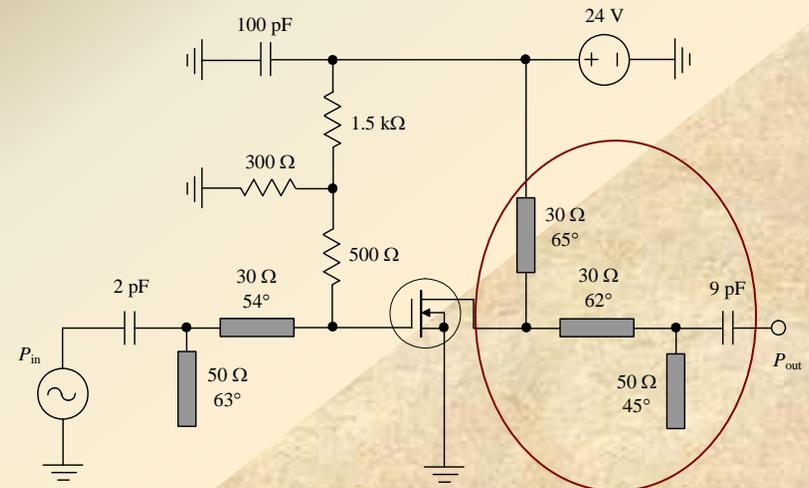


Output matching

Drain voltage and current waveforms



- **output power - 39 dBm or 8 W**
- **collector efficiency - 71%**



Load network with output matching

Optimum load network resistances at fundamental for different classes of operation

Class B :
$$R^{(B)} = \frac{V_{cc}}{I_1} = \frac{V_{cc}^2}{2P_1}$$

Class F :
$$R^{(F)} = \frac{4}{\pi} \frac{V_{cc}}{I_1} = \frac{4}{\pi} R^{(B)}$$

Inverse Class F :
$$R^{(invF)} = \frac{\pi}{2} \frac{V_{cc}}{I_1} = \frac{\pi^2}{8} R^{(F)} = \frac{\pi}{2} R^{(B)}$$

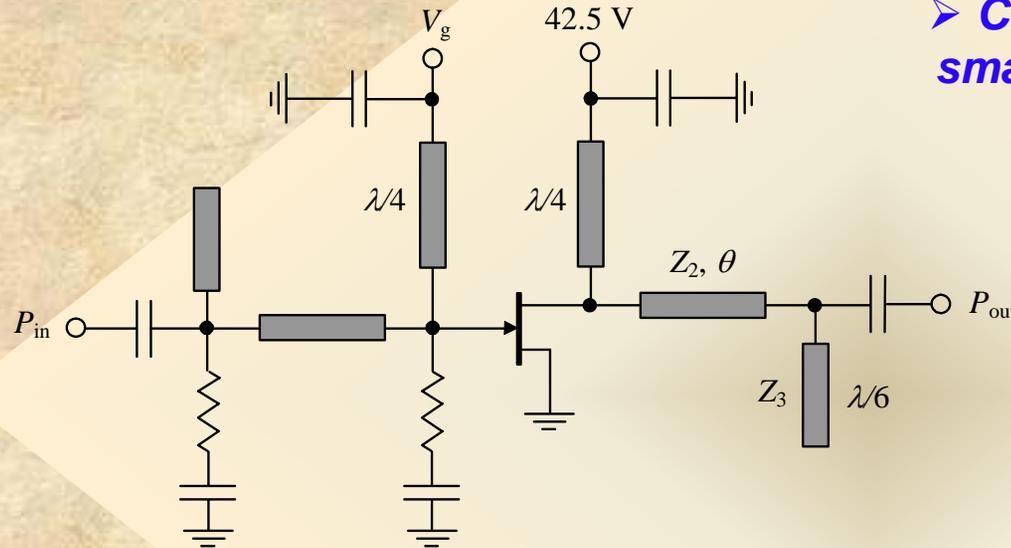
**Load resistance in inverse Class F
is the highest
(1.6 times larger than in Class B)**



**Less impedance
transformation ratio
and easier matching
procedure**

8. Practical high-efficiency RF and microwave Class F power amplifiers

Class F GaN HEMT power amplifier with input harmonic control



➤ *Class AB biasing with small quiescent current*

➤ *RC-circuits at the input for stable operation*

➤ *characteristic impedance Z_2 and electrical length θ is tuned to form third-harmonic tank with output device capacitance C_{ds}*

➤ *characteristic impedances Z_2 and Z_3 are chosen to provide conjugate impedance matching at fundamental*

Input second-harmonic termination circuit is used to provide input quasi-square voltage waveform minimizing device switching time

85% power-added efficiency for 16.5 W at 2 GHz

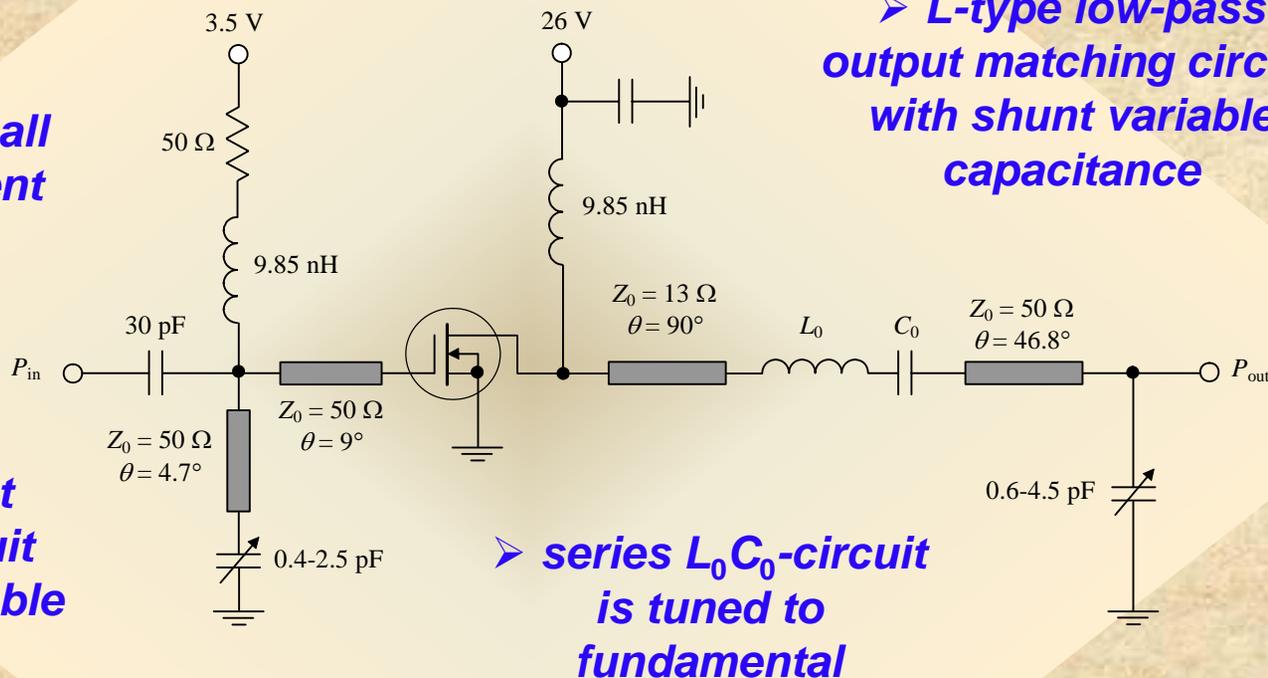
D. Schmelzer and S. I. Long, "A GaN HEMT Class F Amplifier at 2 GHz with > 80% PAE," *IEEE J. Solid-State Circuits*, vol. SC-42, pp. 2130-2136, Oct, 2007.

8. Practical high-efficiency RF and microwave Class F power amplifiers

Inverse Class F LDMOSFET power amplifier with quarterwave line

➤ **Class AB biasing with small quiescent current**

➤ **L-type input matching circuit with shunt variable capacitance**



➤ **L-type low-pass output matching circuit with shunt variable capacitance**

➤ **series $L_0 C_0$ -circuit is tuned to fundamental**

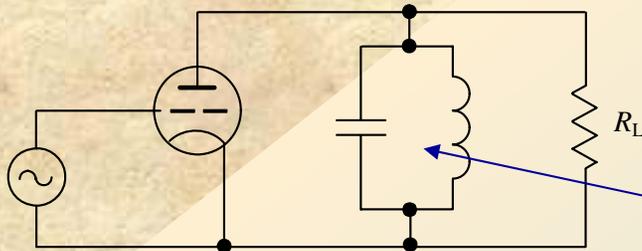
60% drain efficiency for 13 W at 1.78 GHz

F. Lepine, A. Adahl, and H. Zirath, "L-Band LDMOS Power Amplifiers Based on an Inverse Class-F Architecture," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-53, pp. 2007-2012, June 2005.

II. SWITCHED-MODE CLASS E POWER AMPLIFIERS

1. Effect of detuned resonant circuit
2. Basic Class E with shunt capacitance
3. Generalized Class E load network with finite dc-feed inductance
4. Parallel-circuit Class E
5. Class E approximation with transmission lines
6. Class E with quarterwave transmission line
7. Broadband Class E circuit design
8. Practical RF and microwave Class E power amplifiers

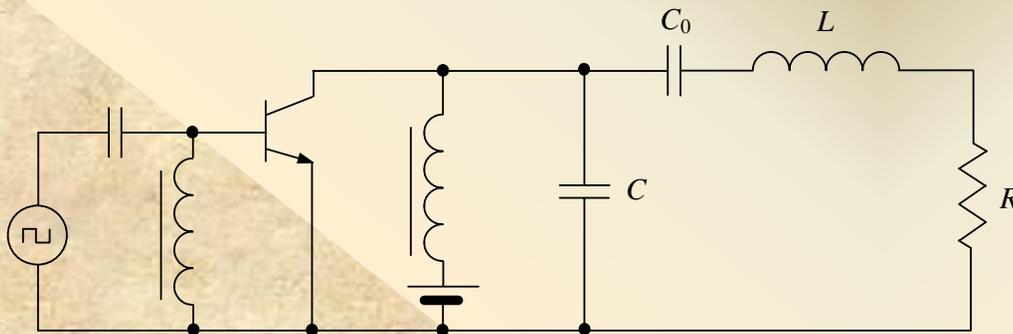
1. Effect of detuned resonant circuit



- anode efficiency of 92-93% for resonant-circuit phase angles of 30-40°: inductive impedance at fundamental and capacitive at harmonics

resonant frequency $f \approx (1.4-1.5)f_0$
 f_0 – fundamental frequency

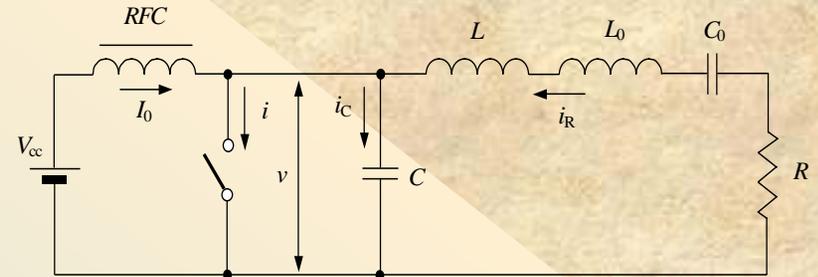
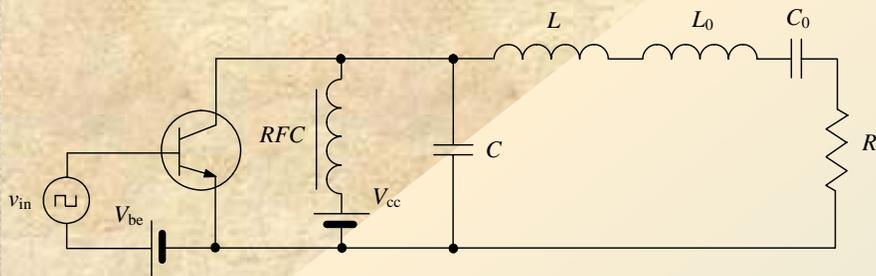
E. P. Khmelnitsky, *Operation of Vacuum-Tube Generator on Detuned Resonant Circuit* (in Russian), Moskva: Svyazizdat, 1962.



- load current lags collector voltage so that series LC_0 -circuit must appear inductive at operating frequency
- pulsed excitation with highest efficiency for conduction angles less than 180°
- collector efficiency of 94% for 20 W 500 kHz bipolar power amplifier with 50% duty cycle

G. D. Ewing, *High-Efficiency Radio-Frequency Power Amplifiers*, Ph.D. Dissertation, Oregon State University, June 1964.

2. Basic Class E with shunt capacitance



Idealized assumptions for analysis:

- **transistor has zero saturation voltage, zero on-resistance, infinite off-resistance and its switching action is instantaneous and lossless**
- **RF choke allows only dc current and has no resistance**
- **total shunt capacitance is assumed to be linear**
- **reactive elements in load network are lossless**
- **loaded quality factor Q_L of series fundamentally tuned resonant L_0C_0 -circuit is infinite to provide pure sinusoidal current flowing into load**
- **for optimum operation 50% duty cycle is used**

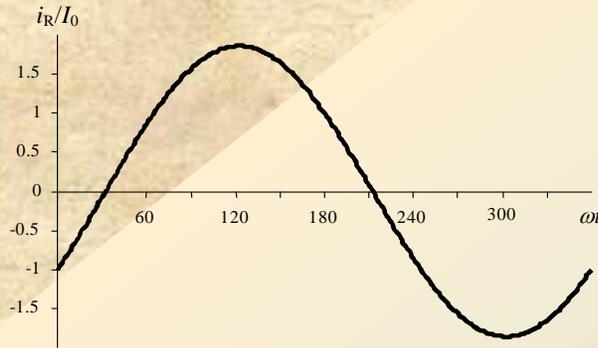
Idealized optimum or nominal conditions

$$v(\omega t) \Big|_{\omega t=2\pi} = 0$$

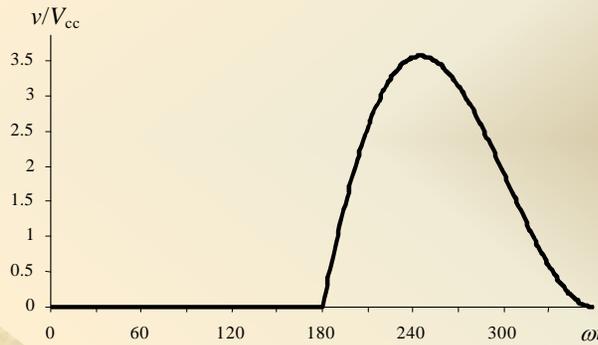
$$\frac{dv(\omega t)}{d\omega t} \Big|_{\omega t=2\pi} = 0$$

2. Basic Class E with shunt capacitance

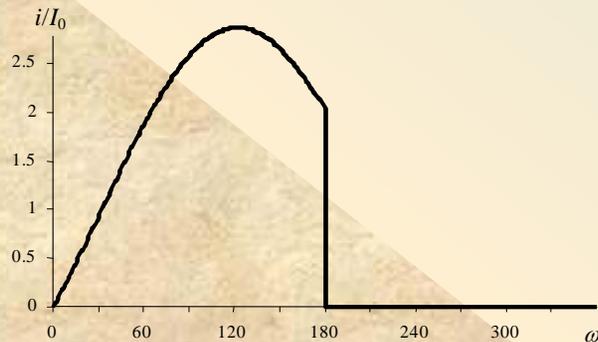
Load current



Collector voltage



Collector current



Optimum circuit parameters :

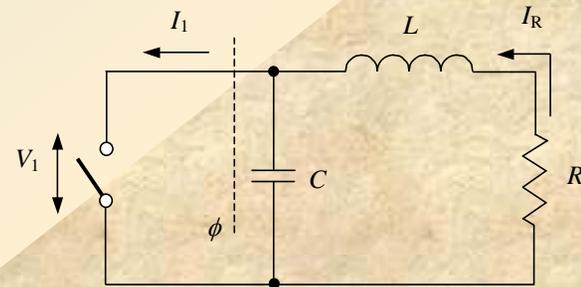
$$L = 1.1525 \frac{R}{\omega} \quad \text{- series inductance}$$

$$C = 0.1836 \frac{1}{\omega R} \quad \text{- shunt capacitance}$$

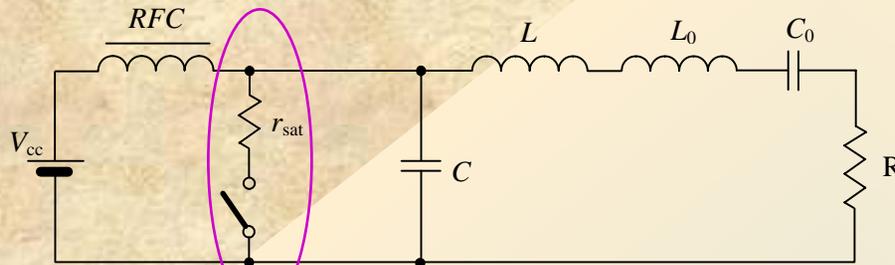
$$R = 0.5768 \frac{V_{cc}^2}{P_{out}} \quad \text{- load resistance}$$

Optimum phase angle at fundamental seen by switch :

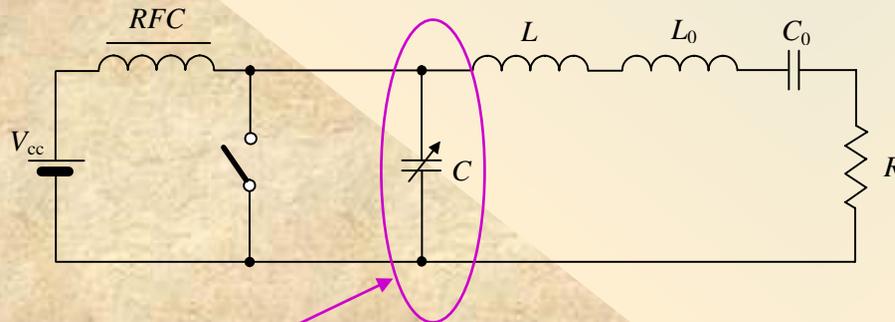
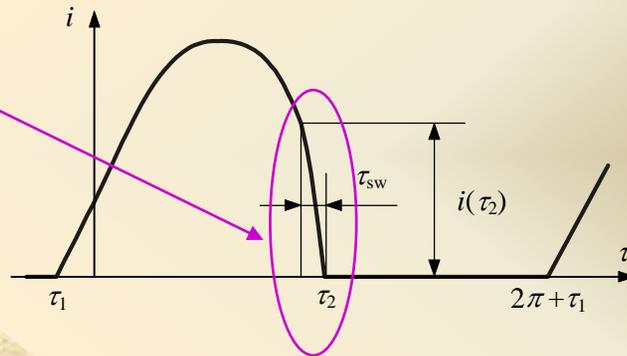
$$\phi = \tan^{-1}\left(\frac{\omega L}{R}\right) - \tan^{-1}\left(\frac{\omega C R}{1 - \frac{\omega L}{R} \omega C R}\right) = 35.945^\circ$$



2. Basic Class E with shunt capacitance



Non-ideal switch



Nonlinear capacitance

Power loss due to non-zero saturation resistance

$$\frac{P_{\text{sat}}}{P_{\text{dc}}} \cong \frac{8}{3} \frac{r_{\text{sat}} P_{\text{out}}^2}{V_{\text{cc}}^2} \cong 1.365 \frac{r_{\text{sat}}}{R}$$

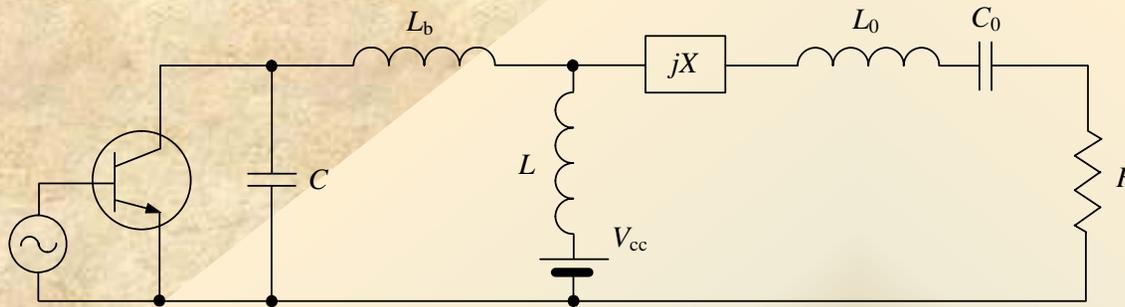
Power loss due to finite switching time

$$\frac{P_{\text{sw}}}{P_{\text{dc}}} \cong \frac{\tau_{\text{sw}}^2}{12}$$

**For $\tau_{\text{sw}} = 0.35$ or 20°
only 1% efficiency loss**

For nonlinear capacitances represented by abrupt junction collector capacitance with $\gamma = 0.5$, peak collector voltage increases by 20%

3. Generalized Class E load network with finite dc-feed inductance



$$i_R(\omega t) = I_R \sin(\omega t + \varphi) - \text{sinusoidal current in load}$$

Optimum ideal voltage conditions across switch:

$$v(\omega t) \Big|_{\omega t=2\pi} = 0$$
$$\frac{dv(\omega t)}{d\omega t} \Big|_{\omega t=2\pi} = 0$$

- **load network consists of dc-feed inductance L supplying also dc current, shunt capacitor C , series reactance X , bondwire inductance L_b , series fundamentally tuned $L_0 C_0$ resonant circuit, and load R**
- **shunt capacitor C can represent intrinsic device output capacitance and external circuit capacitance**
- **active device is considered as ideal switch to provide instantaneous device switching between its on-state and off-state operation conditions**
- **series reactance X can be positive (inductance), zero and negative (capacitive)**

3. Generalized Class E load network with finite dc-feed inductance

$$\omega^2(L + L_b)LC \frac{d^2v(\omega t)}{d(\omega t)^2} + v(\omega t) - V_{cc} - \omega LI_R \cos(\omega t + \varphi) = 0$$

- **second-order differential equation**



$$\frac{v(\omega t)}{V_{cc}} = C_1 \cos(q\omega t) + C_2 \sin(q\omega t) + 1 - \frac{q^2 p}{1 - q^2} \cos(\omega t + \varphi)$$

where $q = 1/\omega\sqrt{(L + L_b)C}$, $p = \frac{\omega LI_R}{V_{cc}}$,

and coefficients C_1 and C_2 are defined from initial conditions

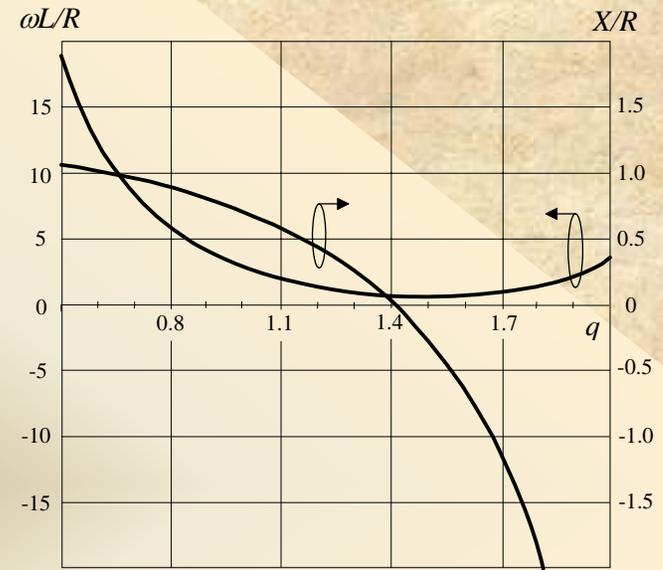
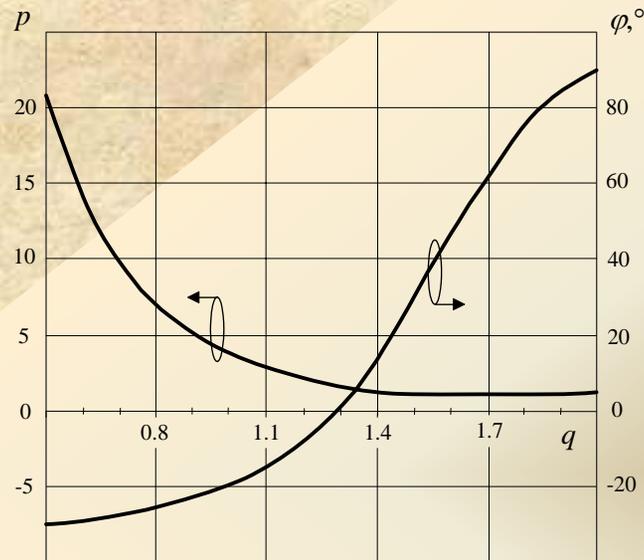
$$\omega CR = 1/q^2 \left(1 + \frac{L_b}{L}\right) \frac{\omega L}{R} \quad \text{- shunt capacitance}$$

$$\frac{\omega L}{R} = p \left(1 + \frac{L_b}{L}\right) / \left(\frac{\pi}{2p} + \frac{2}{\pi} \cos \varphi - \sin \varphi\right) \quad \text{- dc-feed inductance}$$

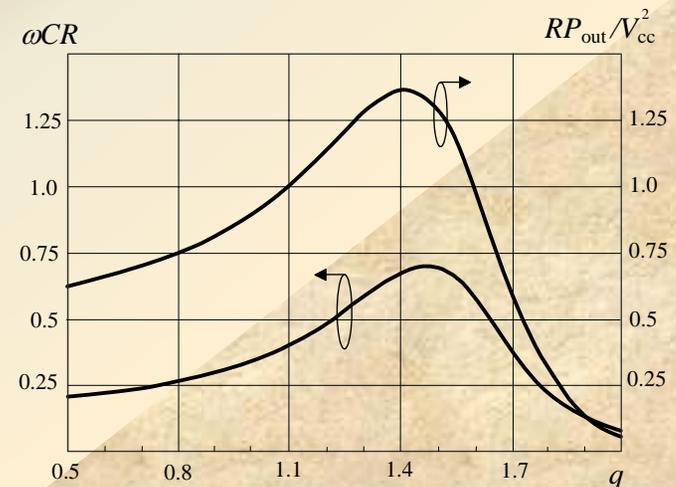
$$R = \frac{1}{2\pi^2} \left(\frac{\pi^2}{2p} + 2 \cos \varphi - \pi \sin \varphi\right)^2 \frac{V_{cc}^2}{P_{out}} / \left(1 + \frac{L_b}{L}\right)^2 \quad \text{- load resistance}$$

3. Generalized Class E load network with finite dc-feed inductance

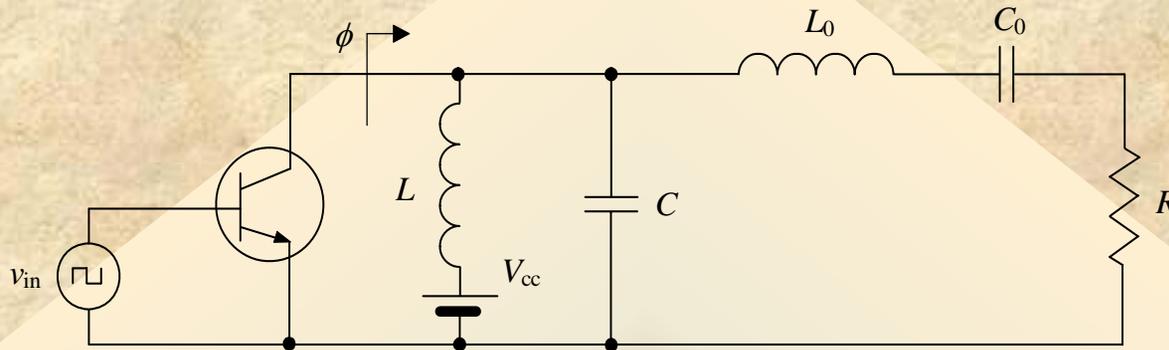
Normalized load network parameters versus $q = 1/\omega\sqrt{LC}$, $L_b = 0$



- $q \leq 0.5$: close to Class E with shunt capacitance with positive (inductive) series reactance ($X > 0$)
- $q = 1.412$: parallel-circuit Class E with zero reactance ($X = 0$) – maximum load resistance R
- $q = 1.468$: maximum shunt capacitance C (maximum operating frequency f_{\max}) with negative (capacitive) reactance ($X < 0$)



4. Parallel-circuit Class E



To define three unknown parameters q , ϕ and p , two ideal optimum conditions and third equation for zero reactive part of fundamental Fourier component are applied resulting to system of three algebraic equations:

$$v(\omega t) \Big|_{\omega t=2\pi} = 0 \quad \frac{dv(\omega t)}{d\omega t} \Big|_{\omega t=2\pi} = 0$$

$$V_X = -\frac{1}{\pi} \int_0^{2\pi} v(\omega t) \cos(\omega t + \phi) d(\omega t) = 0$$

$$q = 1.412 \quad p = 1.210$$

$$\phi = 15.155^\circ$$

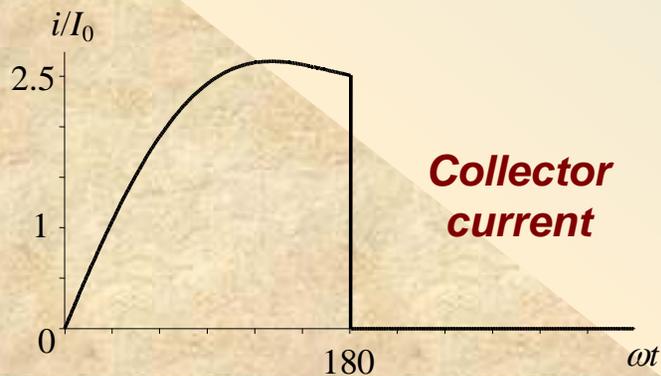
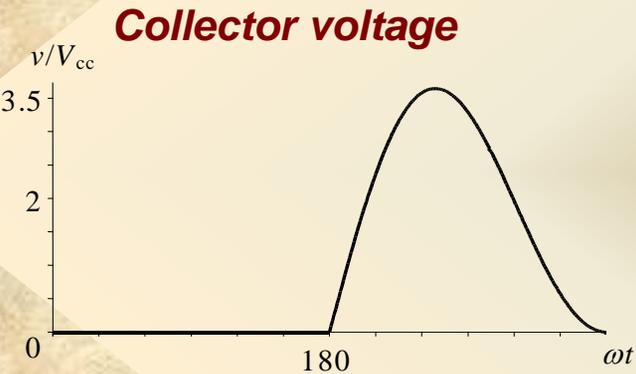
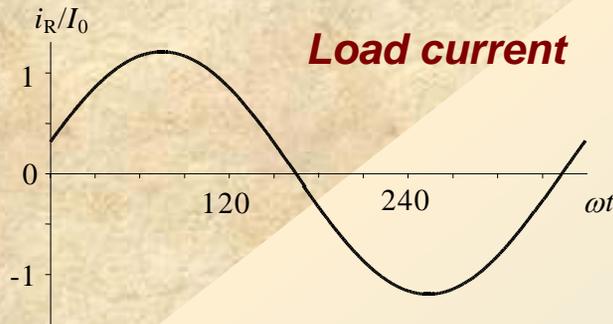
Optimum circuit parameters :

$$L = 0.732 \frac{R}{\omega} \quad \text{- parallel inductance}$$

$$C = \frac{0.685}{\omega R} \quad \text{- parallel capacitance}$$

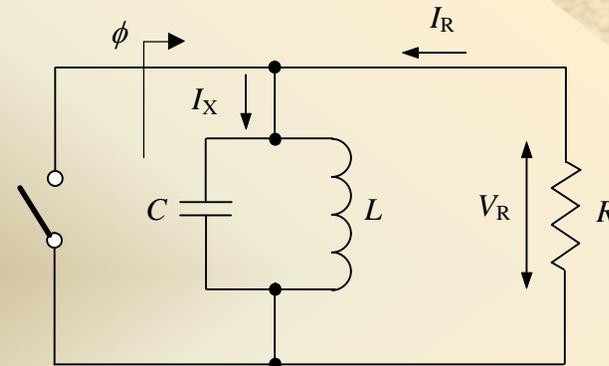
$$R = 1.365 \frac{V_{cc}^2}{P_{out}} \quad \text{- load resistance: highest value in Class E}$$

4. Parallel-circuit Class E

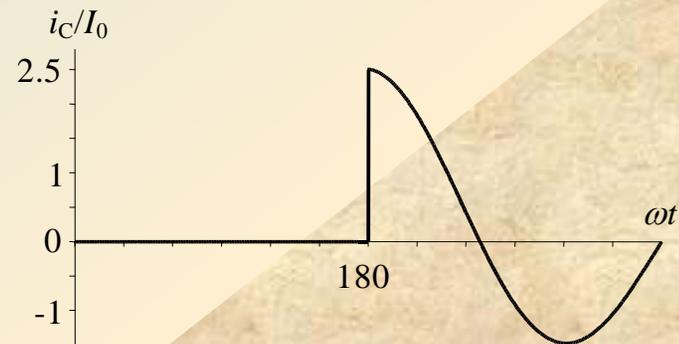


Inductive impedance at fundamental

$$\phi = \tan^{-1}\left(\frac{I_X}{I_R}\right) = \tan^{-1}\left(\frac{R}{\omega L} - \omega RC\right) = 34.244^\circ$$

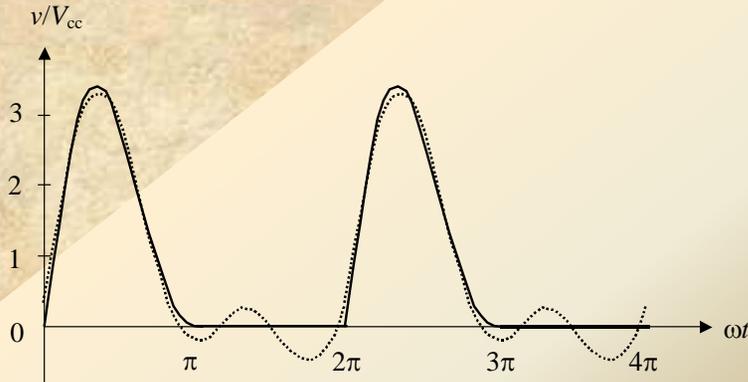


Current through capacitance



5. Class E with transmission lines: approximation

Two-harmonic collector voltage approximation

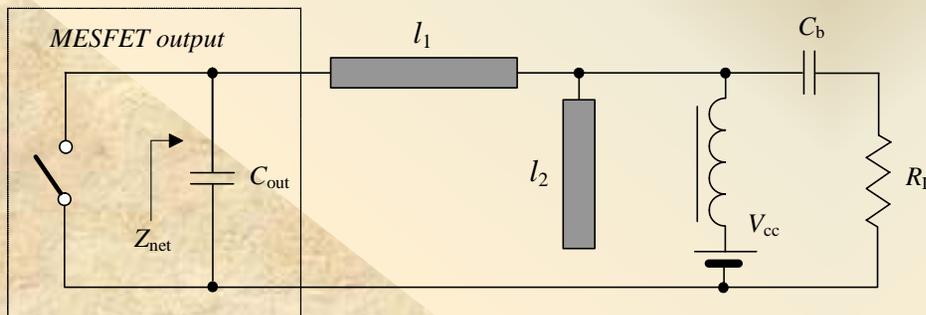


Optimum impedance at fundamental seen by device :

$$Z_{\text{net1}} = R \left(1 + j \tan 49.052^\circ \right)$$

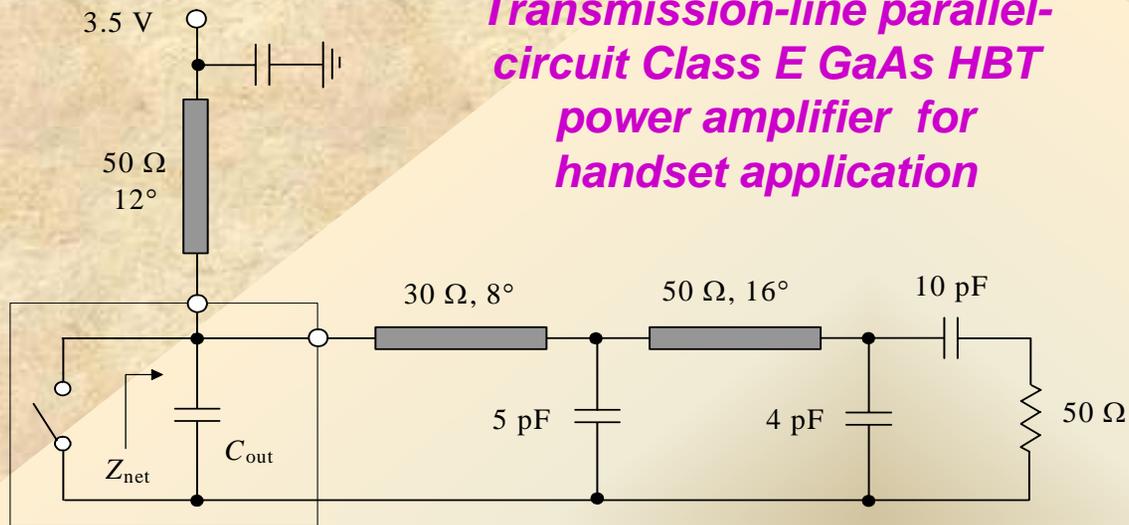
➤ electrical lengths of transmission lines l_1 and l_2 should be of 45° to provide open circuit seen by device at second harmonic

➤ transmission-line characteristic impedances are chosen to provide optimum inductive impedance seen by device output at fundamental

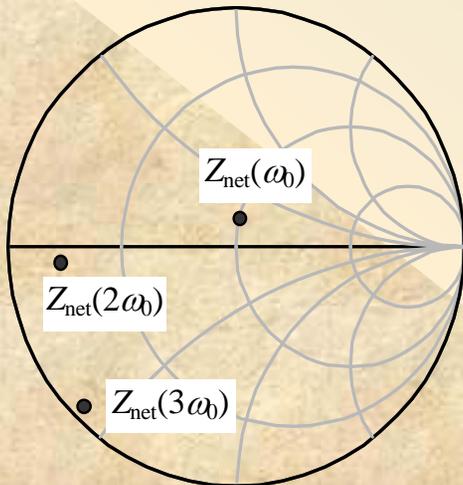


T. B. Mader and Z. B. Popovic, "The Transmission-Line High-Efficiency Class-E Amplifier," *IEEE Microwave and Guided Wave Lett.*, vol. 5, pp. 290-292, Sept. 1995

5. Class E with transmission lines: approximation



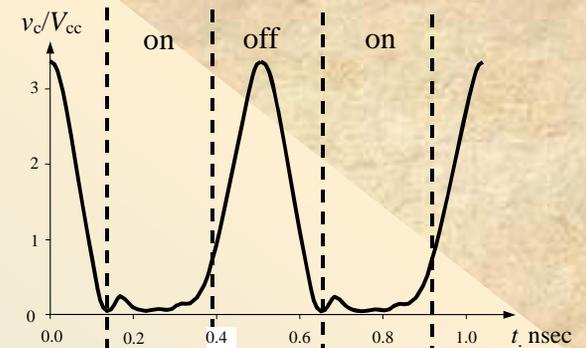
Transmission-line parallel-circuit Class E GaAs HBT power amplifier for handset application



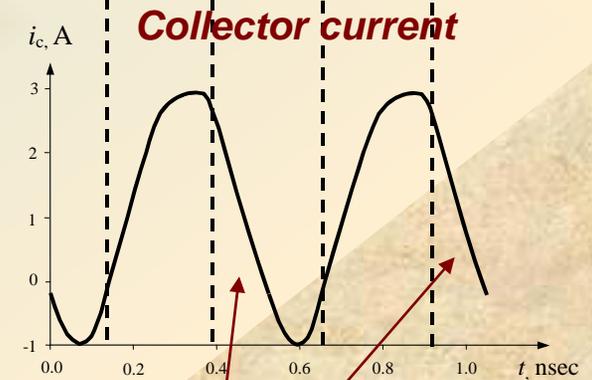
➤ **parameters of parallel transmission line is chosen to realize optimum inductive impedance at fundamental**

➤ **output matching circuit consisting of series microstrip line with two shunt capacitors should provide capacitive reactances at second and third harmonics**

Collector voltage

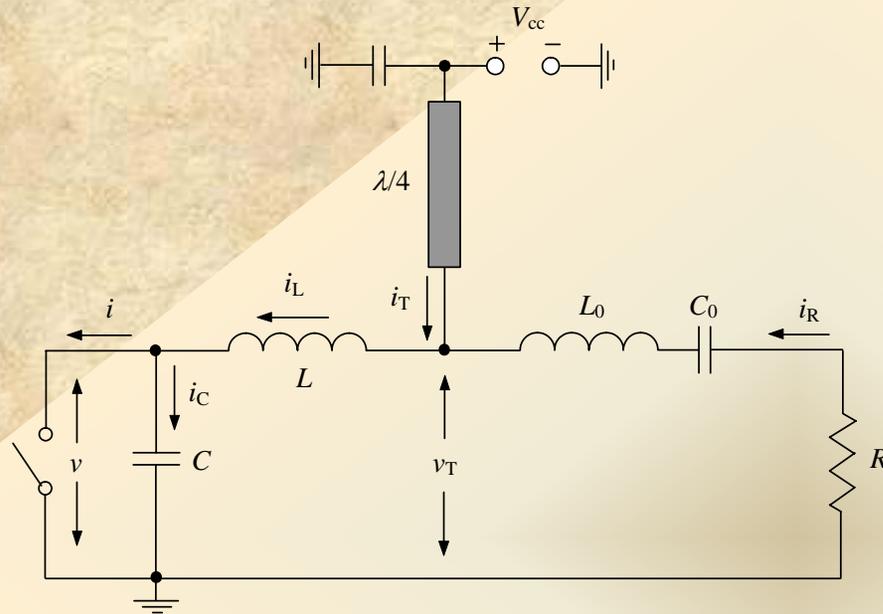


Collector current



Current flowing through collector capacitor

6. Class E with quarterwave transmission line



**Optimum voltage conditions
across switch:**

$$v(\omega t) \Big|_{\omega t=2\pi} = 0$$

$$\frac{dv(\omega t)}{d\omega t} \Big|_{\omega t=2\pi} = 0$$

➤ **sinusoidal load current**

➤ **50% duty cycle**

$$\frac{d^2 i_C(\omega t)}{d(\omega t)^2} + \frac{q^2}{2} i_C(\omega t) + I_R \sin(\omega t + \varphi) = 0 \quad \text{- second-order differential equation}$$

Boundary conditions:

$$i_C(\omega t) \Big|_{\omega t=\pi} = 2i_R(\pi)$$

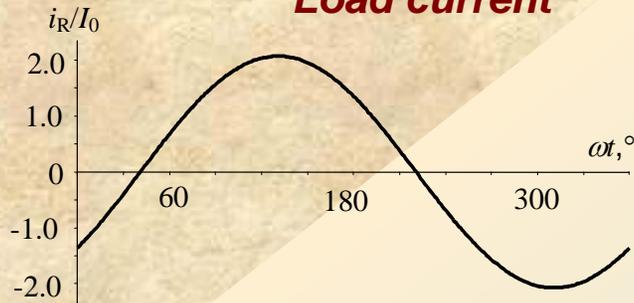
$$\frac{di_C(\omega t)}{d(\omega t)} \Big|_{\omega t=\pi} = \frac{V_{cc}}{\omega L} - I_R \cos(\varphi)$$

$$p = \frac{\omega L I_R}{V_{cc}} \quad q = 1/\omega \sqrt{LC}$$

$$q = 1.649 \quad p = 1.302 \quad \varphi = -40.8^\circ$$

6. Class E with quarterwave transmission line

Load current



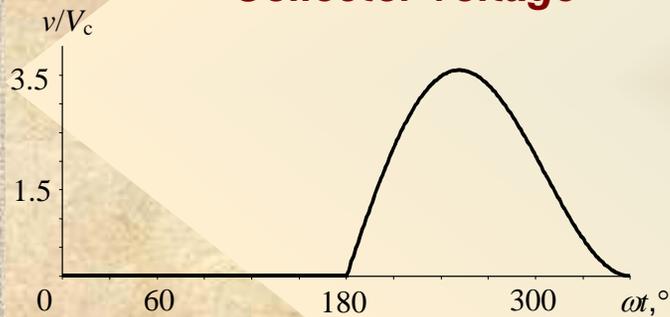
Optimum circuit parameters :

$$L = 1.349 \frac{R}{\omega} \quad \text{- series inductance}$$

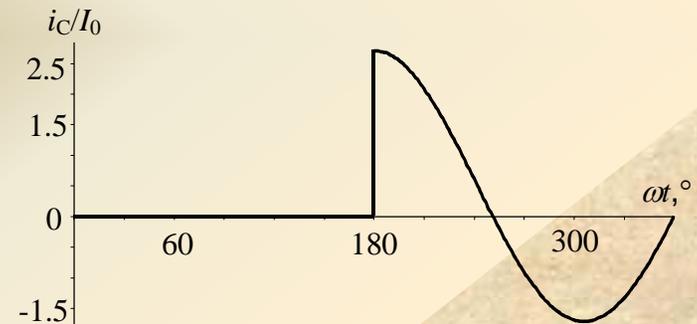
$$C = \frac{0.2725}{\omega R} \quad \text{- shunt capacitance}$$

$$R = 0.465 \frac{V_{cc}^2}{P_{out}} \quad \text{- load resistance}$$

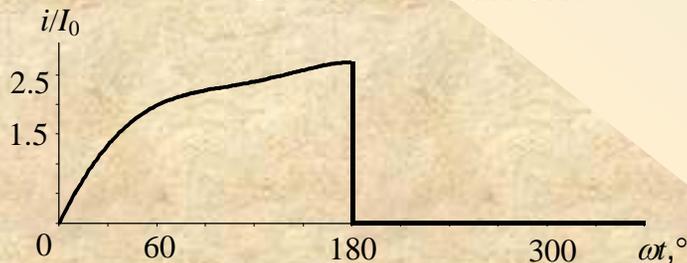
Collector voltage



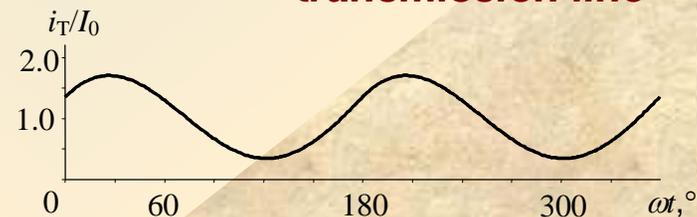
Current through capacitance



Collector current

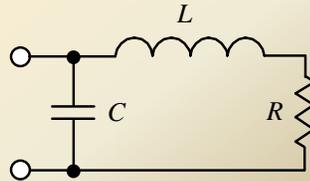
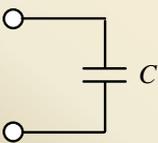
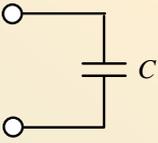
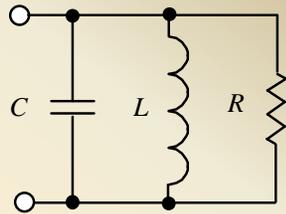
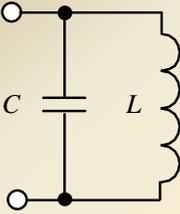
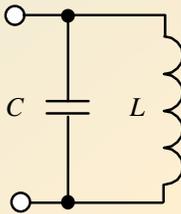
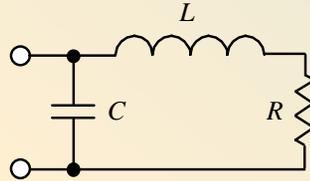
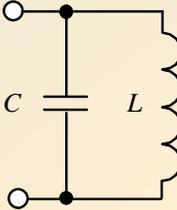
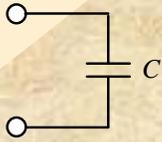


Current through transmission line



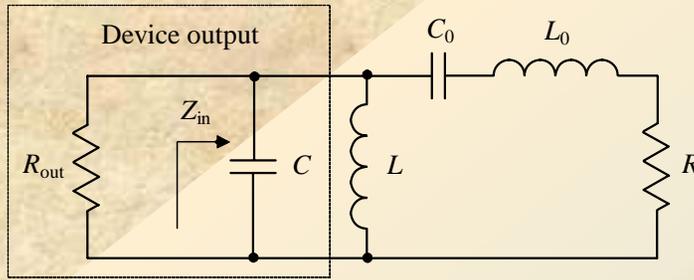
6. Class E with quarterwave transmission line

Optimum impedances at fundamental and harmonics for different Class E load networks

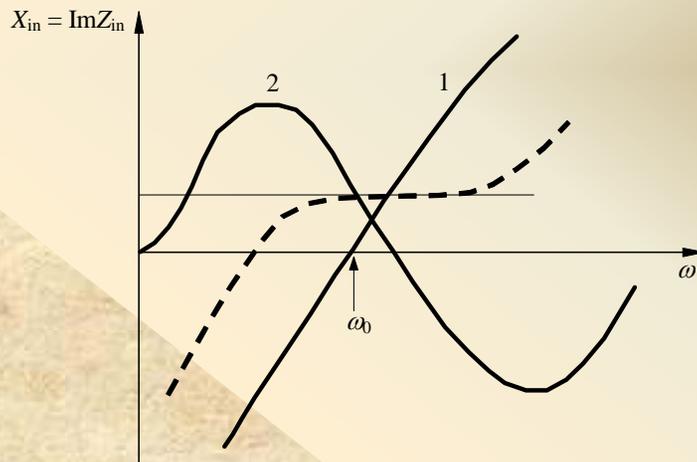
Class E load network	f_0 (fundamental)	$2nf_0$ (even harmonics)	$(2n+1)f_0$ (odd harmonics)
Class E with shunt capacitance			
Class E with parallel circuit			
Class E with quarterwave transmission line			

7. Broadband Class E circuit design

Reactance compensation load network



Reactance compensation principle



1 - impedance provided by series $L_0 C_0$ resonant circuit 2 - impedance provided by parallel LC resonant circuit

➤ summation of reactances with opposite slopes results in constant load phase over broad frequency range

Input load network admittance

$$Y_{in} = \left(j\omega C + \frac{1}{j\omega L} + \frac{1}{R + j\omega' L_0} \right)$$

$$\omega' = \omega \left(1 - \frac{\omega_0^2}{\omega^2} \right) \quad \omega_0 = 1/\sqrt{L_0 C_0}$$

To maximize bandwidth:

$$\left. \frac{d \operatorname{Im} Y_{in}(\omega)}{d\omega} \right|_{\omega=\omega_0} = 0$$



$$C + \frac{1}{\omega^2 L} - \frac{2L_0}{R^2} = 0$$

Optimum parameters for series resonant circuit in Class E mode

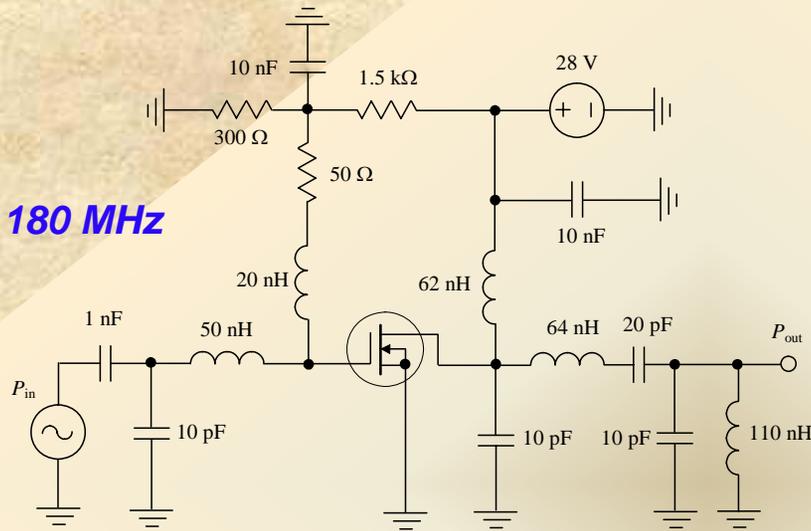
$$L_0 = 1.026 \frac{R}{\omega}$$

$$C_0 = 1/\omega^2 L_0$$

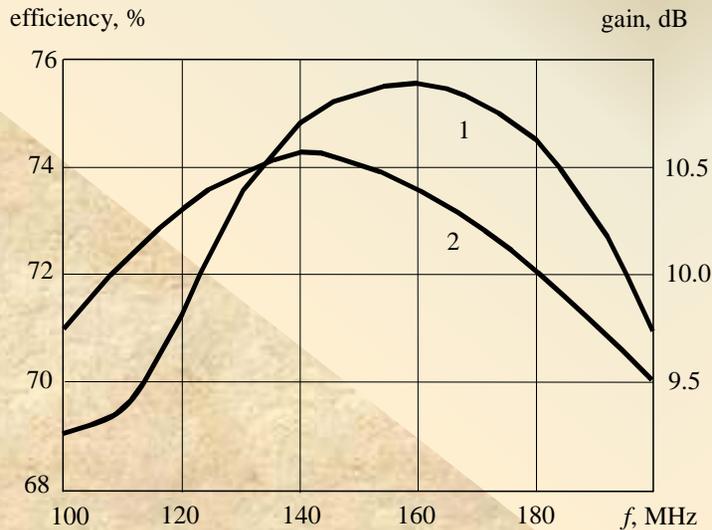
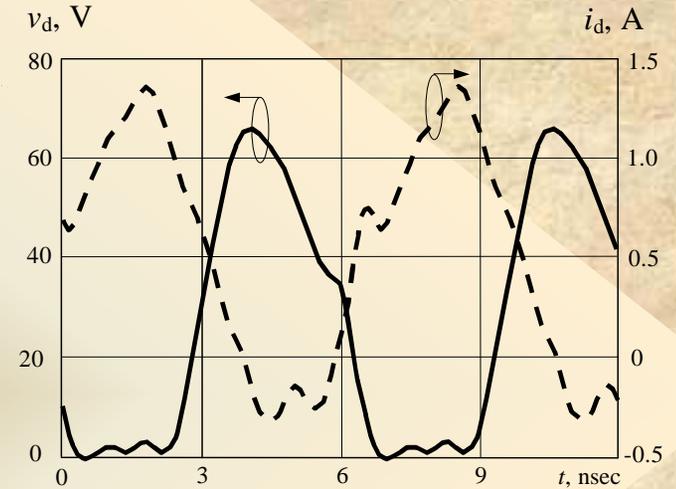
7. Broadband Class E circuit design

Broadband Class E power amplifier with reactance compensation

$f_0 = 120...180$ MHz



Drain voltage and current waveforms



LDMOSFET:

gate length 1.25 μ m
gate width 7x1.44 mm

1 - drain efficiency > 71%

2 - power gain > 9.5 dB

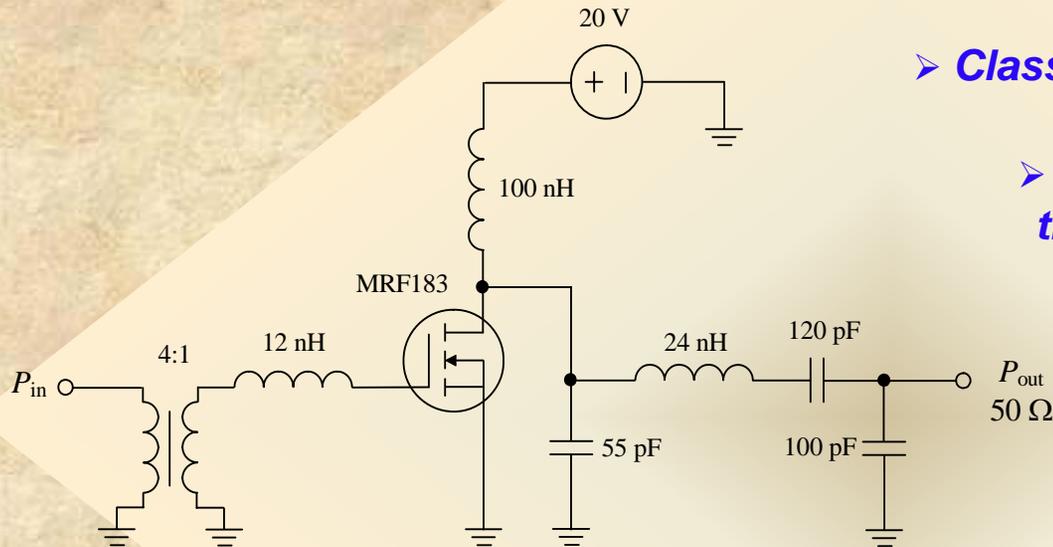
➤ input power - 1 W

➤ input VSWR < 1.4

➤ gain flatness $\leq \pm 0.3$

8. Practical RF and microwave Class E power amplifiers

High power LDMOSFET RF Class E power amplifier



➤ **Class B with zero quiescent current**

➤ **series inductance and ferrite 4:1 transformer is required to match device input impedance**

➤ **L-type output transformer to match optimum 1.5 Ω output impedance to 50 Ω load**

➤ **quality factor of resonant circuit was chosen to be sufficiently low (~ 5) to provide some frequency bandwidth operation and to reduce sensitivity to resonant circuit parameters**

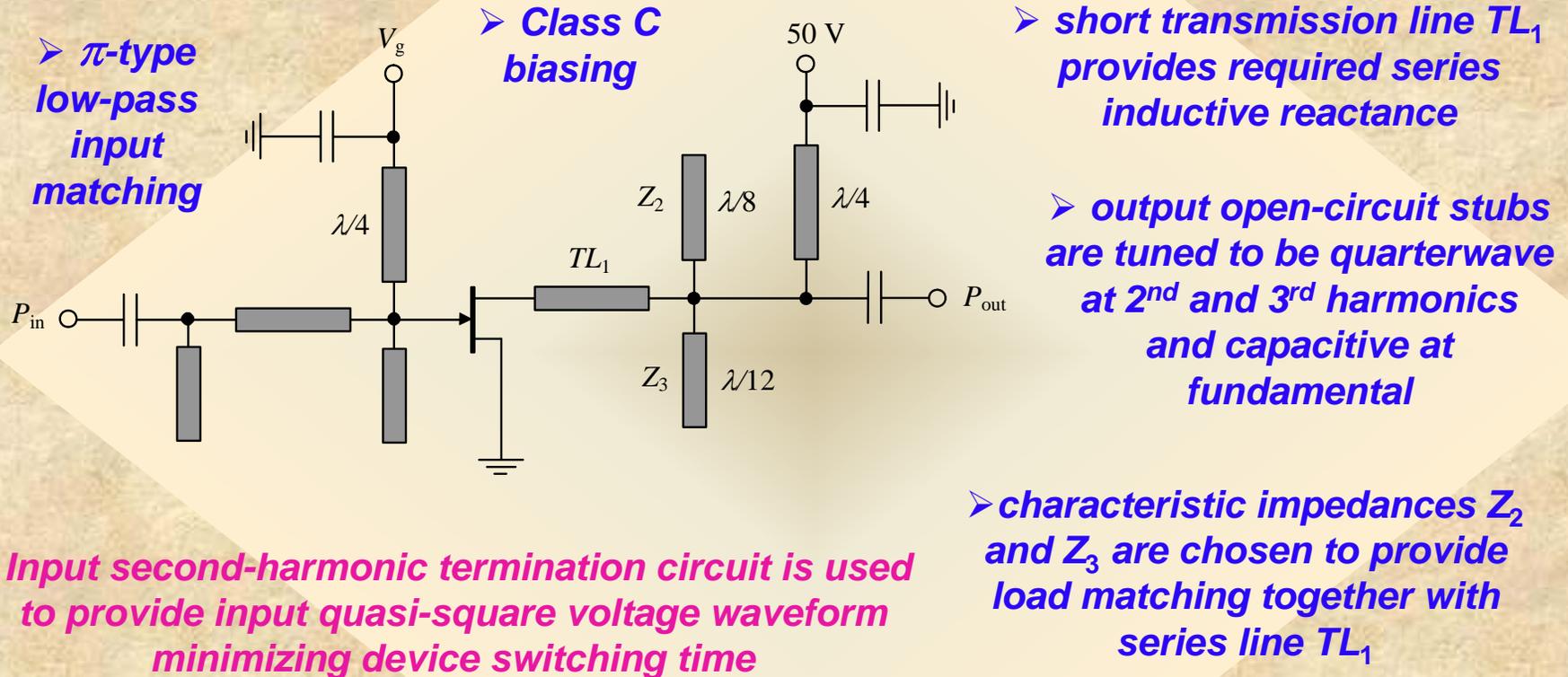
➤ **required value of Class E shunt capacitance is provided by device intrinsic 38 pF capacitance and external 55 pF capacitance**

70% drain efficiency for 54 W at 144 MHz

H. Zirath and D. B. Rutledge, "An LDMOS VHF Class-E Power Amplifier Using a High-Q Novel Variable Inductor," *IEEE Trans. Microwave Theory Techn.*, vol. 47, pp. 359-362, Dec. 1999.

8. Practical RF and microwave Class E power amplifiers

Transmission-line low-harmonic GaN HEMT Class E power amplifier



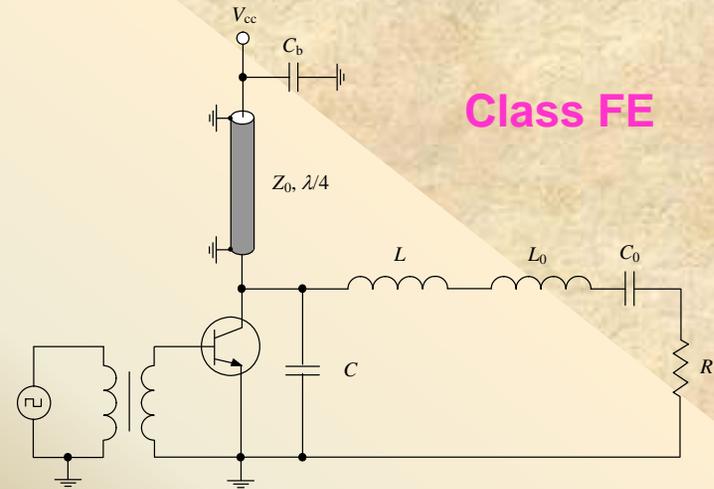
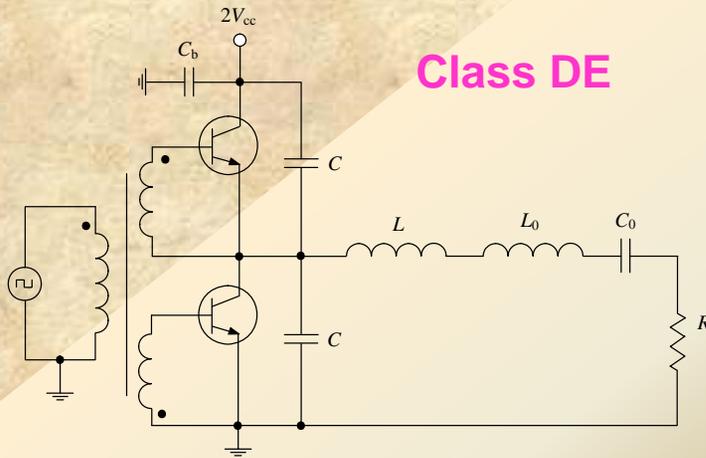
74% power-added efficiency for 11.4 W at 2 GHz

H. G. Bae, R. Negra, S. Boumaiza, and F. M. Ghannouchi, "High-Efficiency GaN Class-E Power Amplifier with Compact Harmonic-Suppression Network," Proc. 37th European Microwave Conf., pp. 1093-1096, 2007.

III. SWITCHED-MODE CLASS FE POWER AMPLIFIERS

1. Basic load network and operation principle
2. Load network parameters and voltage and current waveforms
3. Design approximations with second-harmonic control (Class EF_2) and third-harmonic control (Class E/F_3)

1. Basic load network and operation principle



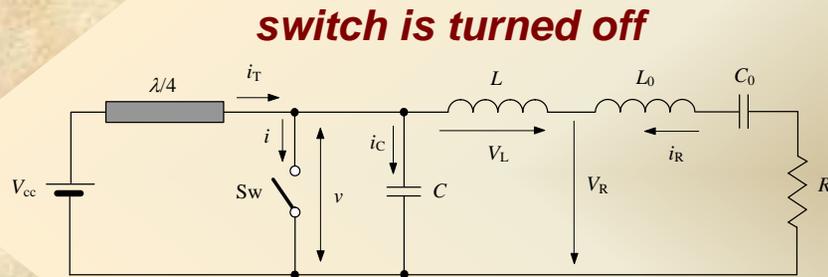
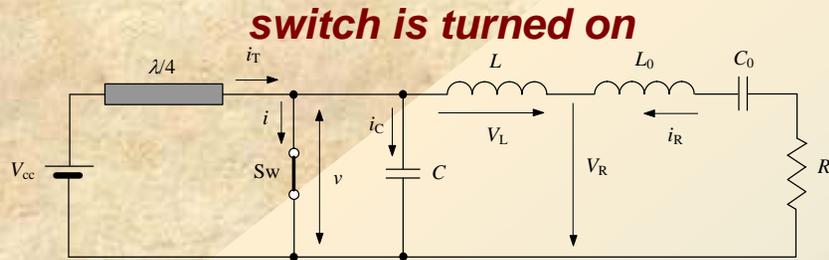
- ***Class E idealized optimum conditions applied to Class F mode affected by shunt parasitic capacitance, with added series inductance***
- ***symmetrizing action of shunt quarterwave line provides its voltage inverter mode resulting in similar waveform as in Class D or Class DE: it stores voltage waveform in traveling wave along its length which returns delayed by one-half fundamental period and inverted due to reflection from short-circuited end***
- ***transistor has zero saturation voltage, zero on-resistance, infinite off-resistance and its switching action is instantaneous and lossless***

Idealized optimum conditions

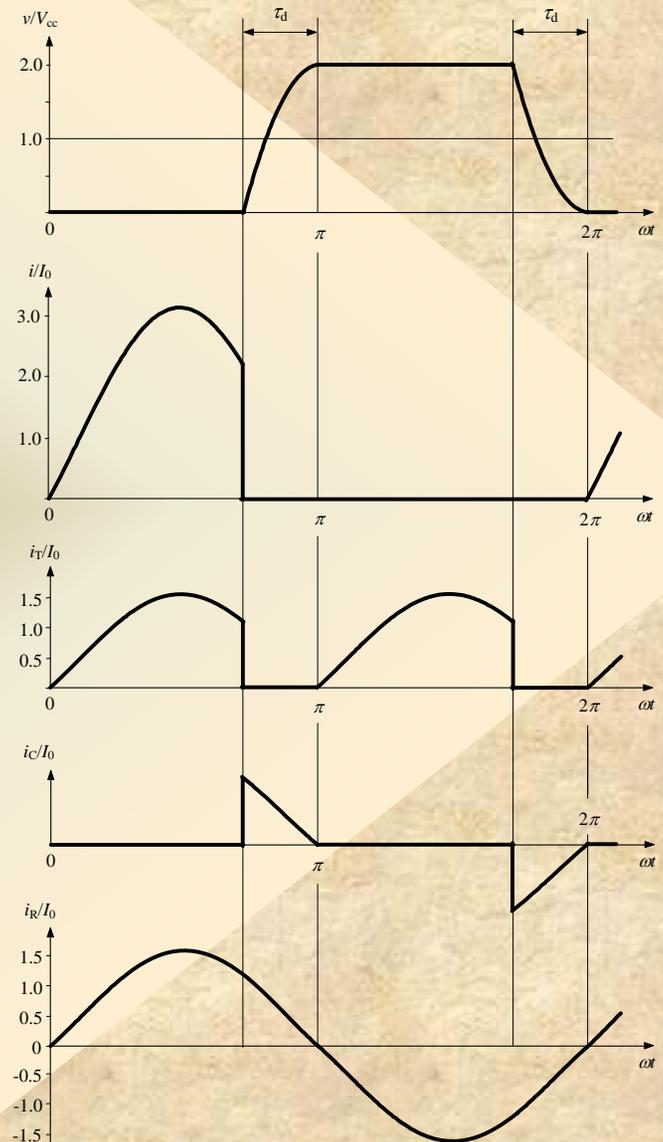
$$v(\omega t) \Big|_{\omega t=2\pi} = 0$$

$$\frac{dv(\omega t)}{d\omega t} \Big|_{\omega t=2\pi} = 0$$

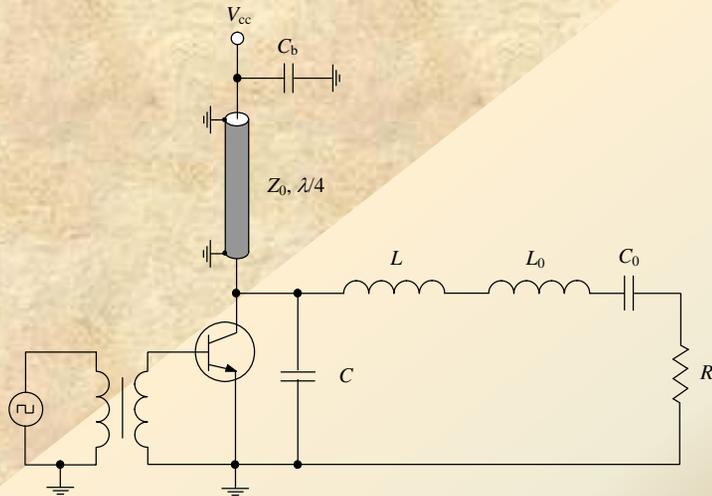
1. Basic load network and operation principle



- **dead time during charging or discharging process when current flow through shunt capacitance**
- **half-wave symmetry of transmission-line current waveform: line attempts to do same work in first and second halves of cycle**
- **zero initial phase and duty cycle $D < 0.5$**



2. Load network parameters and voltage and current waveforms



τ_d - dead time

Optimum circuit parameters :

$$R = \frac{2(1 + \cos \tau_d)^2}{\pi^2} \frac{V_{cc}^2}{P_{out}} \quad \text{- load resistance}$$

$$L = \frac{\tau_d - \sin \tau_d \cos \tau_d}{\sin^2 \tau_d} \frac{R}{\omega} \quad \text{- series inductance}$$

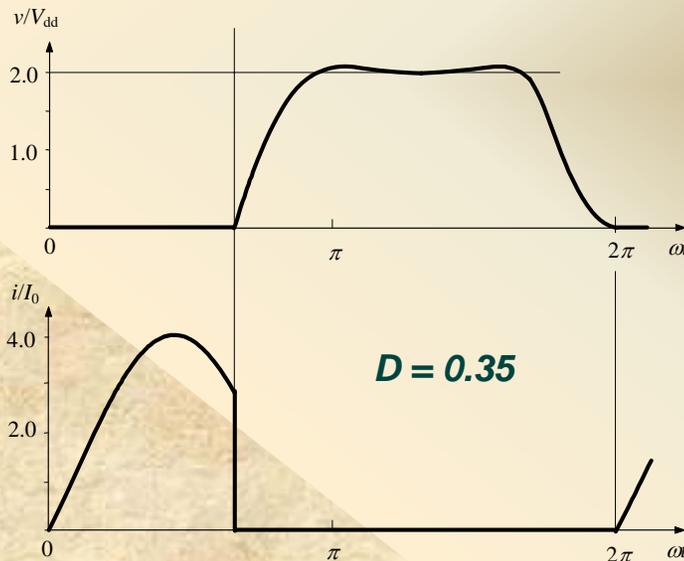
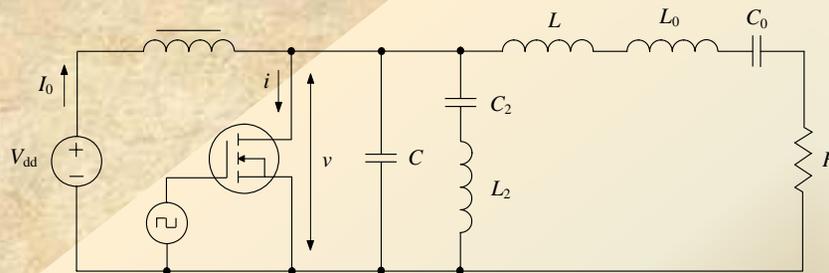
$$C = \frac{\sin^2 \tau_d}{\pi} \frac{1}{\omega R} \quad \text{- shunt capacitance}$$

Optimum impedances at fundamental and harmonics for Class F, Class E and Class FE load networks

High-efficiency mode	f_0 (fundamental)	$2nf_0$ (even harmonics)	$(2n+1)f_0$ (odd harmonics)
Class F with quarterwave line		short	open
Class E with shunt capacitance			
Class FE with quarterwave line		short	

3. Design approximations with second-harmonic control (Class EF_2) and third-harmonic control (Class E/F_3)

Class E_2F (or F_2E) power amplifier



Idealized optimum conditions

$$v(\omega t) \Big|_{\omega t=2\pi} = 0$$

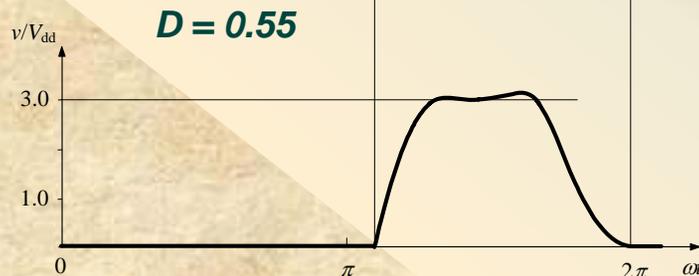
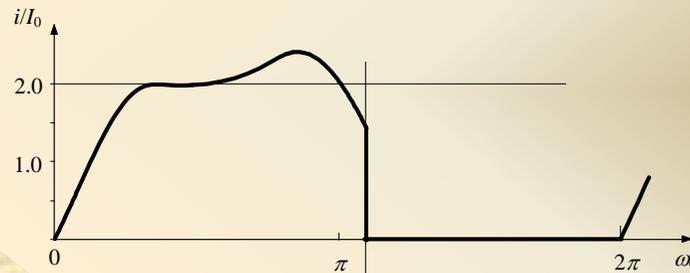
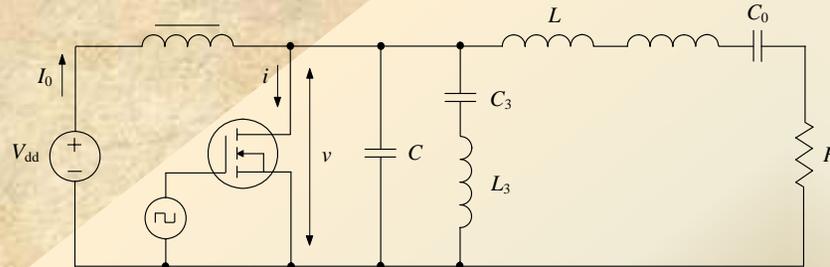
$$\frac{dv(\omega t)}{d\omega t} \Big|_{\omega t=2\pi} = 0$$

- *transistor has zero saturation voltage, zero on-resistance, infinite off-resistance and its switching action is instantaneous and lossless*
- *ideal Class E load network with shunt capacitance*
- *series resonant L_2C_2 circuit tuned to second harmonic*

Z. Kaczmarczyk, "High-Efficiency Class E, EF_2 and E/F_3 Inverters," *IEEE Trans. Industrial Electronics*, vol. IE-53, pp. 1584-1593, Oct. 2006

3. Design approximations with second-harmonic control (Class EF₂) and third-harmonic control (Class E/F₃)

Class E/F₃ power amplifier



Idealized optimum conditions

$$v(\omega t) \Big|_{\omega t=2\pi} = 0$$

$$\frac{dv(\omega t)}{d\omega t} \Big|_{\omega t=2\pi} = 0$$

- transistor has zero saturation voltage, zero on-resistance, infinite off-resistance and its switching action is instantaneous and lossless
- ideal Class E load network with shunt capacitance
- series resonant L₃C₃ circuit tuned to third harmonic

Z. Kaczmarczyk, "High-Efficiency Class E, EF₂ and E/F₃ Inverters," *IEEE Trans. Industrial Electronics*, vol. IE-53, pp. 1584-1593, Oct. 2006

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