

# ***Predistortion Linearization Measurement Results for Power Amplifiers with Memory Effects***

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# Outline

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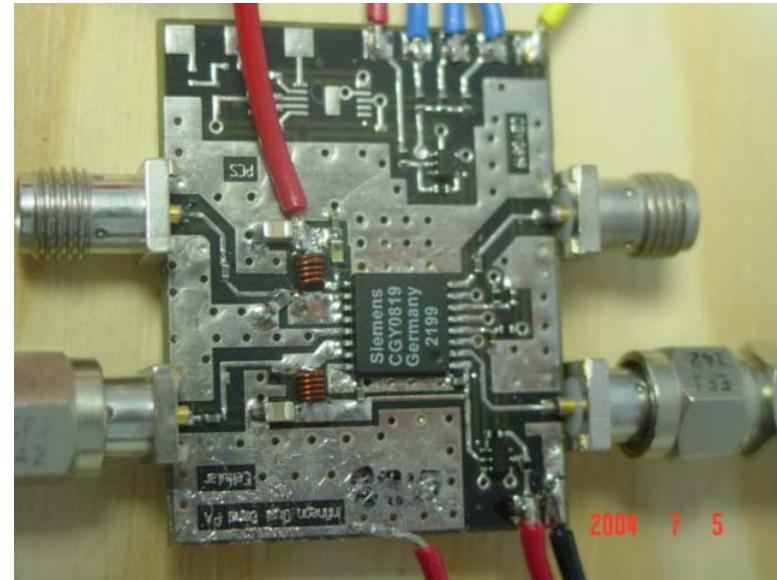
- **Introduction**
  - **Linearity vs. efficiency**
  - **PA memory effects**
- **Digital baseband predistortion (PD)**
  - **Polynomial model**
  - **Orthogonal polynomials**
  - **Memory polynomial model**
- **Test-bed for the digital baseband PD**
- **Measured predistortion linearization results**
- **Conclusions**

# Device Under Test

- Two RF PAs



Ericsson 45 W basestation PA



Siemens 1 W handset PA



# Efficiency vs. Linearity

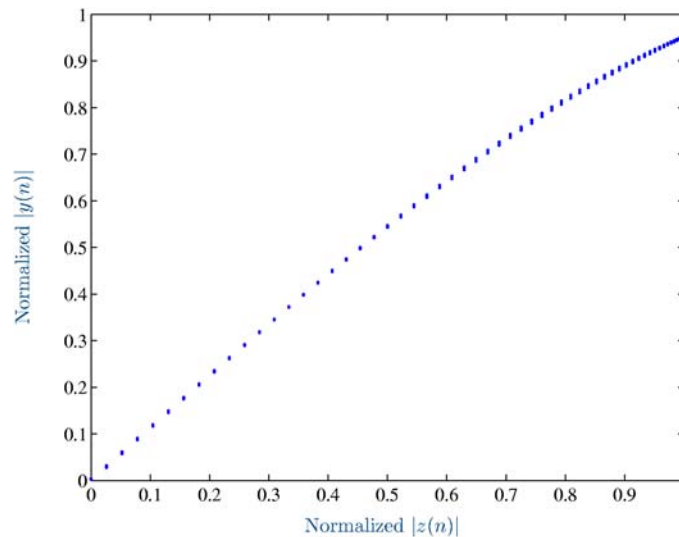
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- The PA efficiency  $\eta = P_{RF}/P_{DC}$ .
- High efficiency PAs are desirable
  - For the handset, long battery life
  - For the base station, reduced operating costs
- High efficiency PAs are usually nonlinear. Nonlinearity causes
  - Spectral regrowth (broadening)
  - In-band distortion and hence increased BER
- PA linearization is often necessary

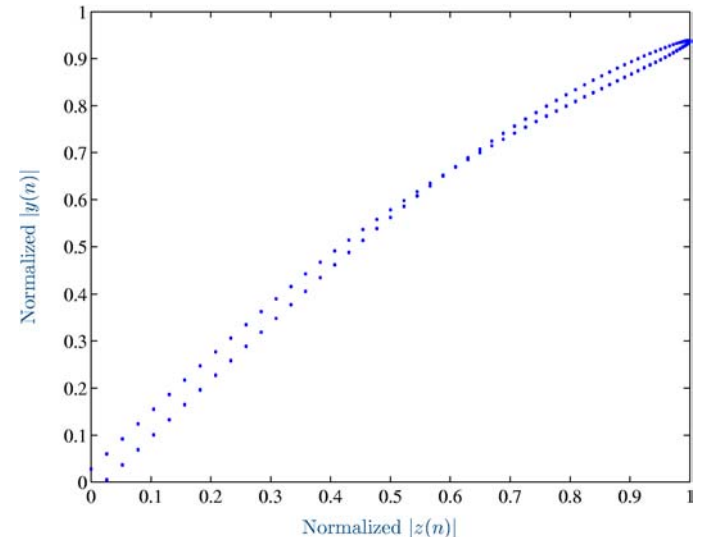


# PA Memory Effects

- For high PAs and/or wideband signals, PA memory effects can be significant.
- Memoryless linearization becomes less effective.
- The hysteresis behavior in the AM/AM response of the Ericsson PA is a sign of memory effects.



AM/AM characteristics of the  
Siemens 1 W PA

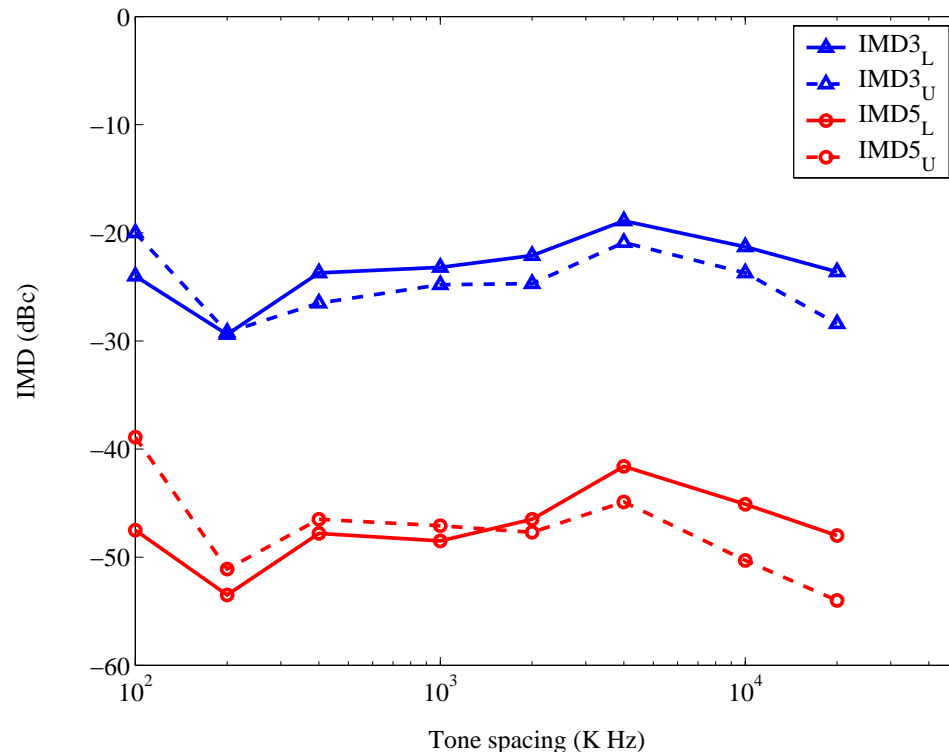


AM/AM characteristics of the  
Ericsson 45 W PA



# PA Memory Effects (Cont'd)

- The asymmetric IMDs in the lower and upper sidebands also indicate memory effects.



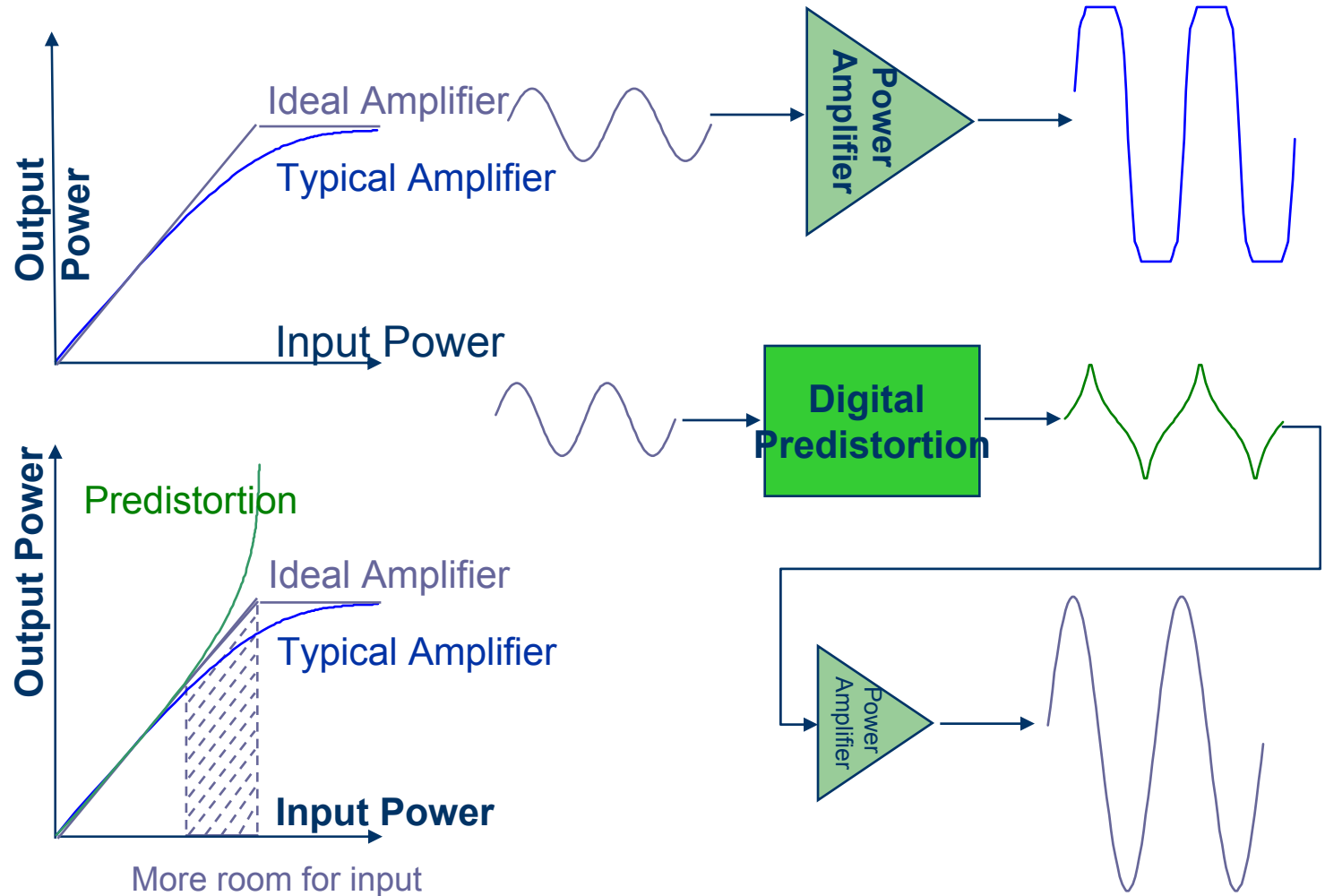
The IMD products vs. tone spacing for the Ericsson 45W PA.

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# Digital Baseband Predistortion





# Memoryless Polynomial Model

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- Memoryless polynomial PD model

$$z(n) = \sum_{k=1}^K a_k x(n) |x(n)|^{k-1}$$

- Can be used to model weak *memoryless* nonlinearities.
- Both even- and odd-order polynomials are included to improve the modeling accuracy [Ding-Zhou'04].
- Typical polynomial order:  $K = 5 \sim 7$ .



# Orthogonal Polynomials

- When  $K$  is large, the regressor matrix in the least-squares coefficient estimation is ill-conditioned and causes numerical instability.
- Orthogonal polynomial basis can be applied to improve the numerical stability [Raich-Qian-Zhou'04]

$$\psi_k(x) = \sum_{l=1}^k \frac{(-1)^{l+k} (k+l)! x |x|^{l-1}}{(l-1)!(l+1)!(k-l)!}$$

- Conv. polynomial basis:  $\phi_k(x) = |x|^{k-1} x$
- Conv. polynomial PD:  $z(n) = \sum_k a_k \phi_k(x(n))$
- Ortho. polynomial PD:  $z(n) = \sum_k \alpha_k \psi_k(x(n))$



# Memory Polynomial Model

- Memory polynomial PD model [Ding et al.'04]

$$z(n) = \sum_{k=1}^K \sum_{q=0}^Q a_{kq} x(n-q) |x(n-q)|^{k-1}.$$

- When  $Q=0$ , memoryless PD
  - Includes memory structure, a special case of Volterra
  - $K(Q+1)$  parameters: simpler than Volterra
  - Simple parameter estimation: linear least-squares
- Orthogonal polynomial basis also helps to improve the numerical stability of the model

$$z(n) = \sum_{k=1}^K \sum_{q=0}^Q \alpha_{kq} \psi_k(x(n-q)).$$

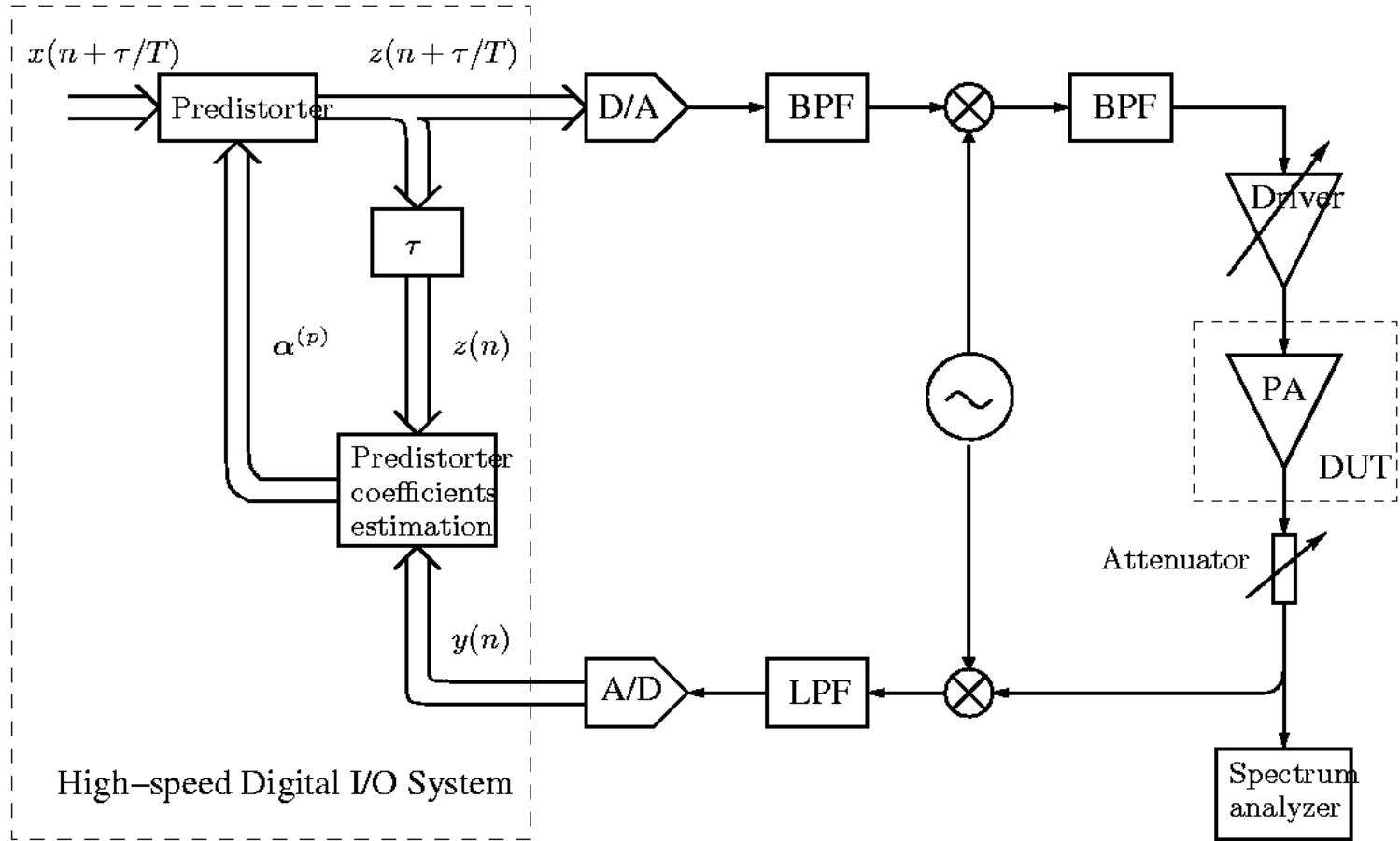


# Outline

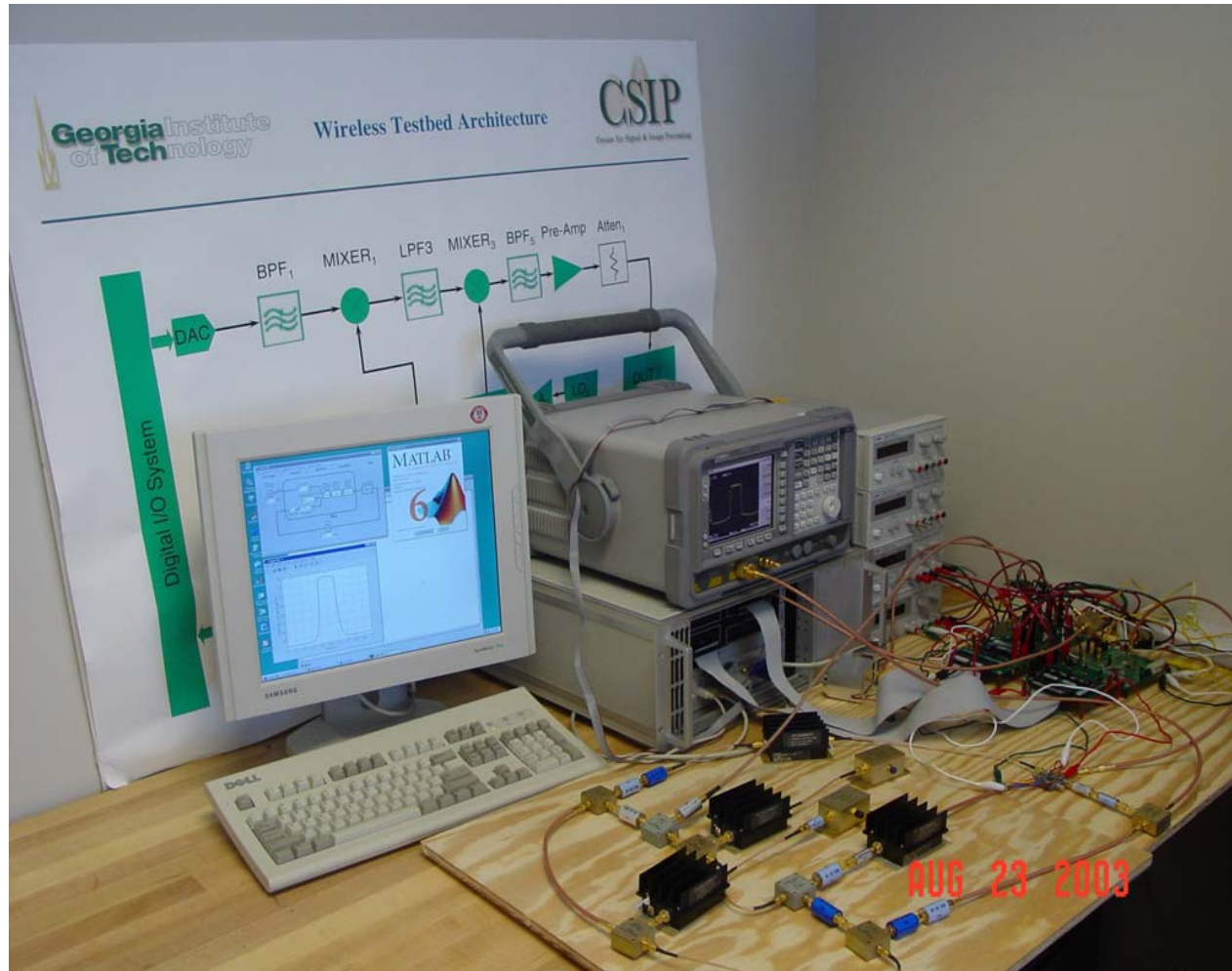
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# System Diagram of the Test-bed



# Test-bed Picture

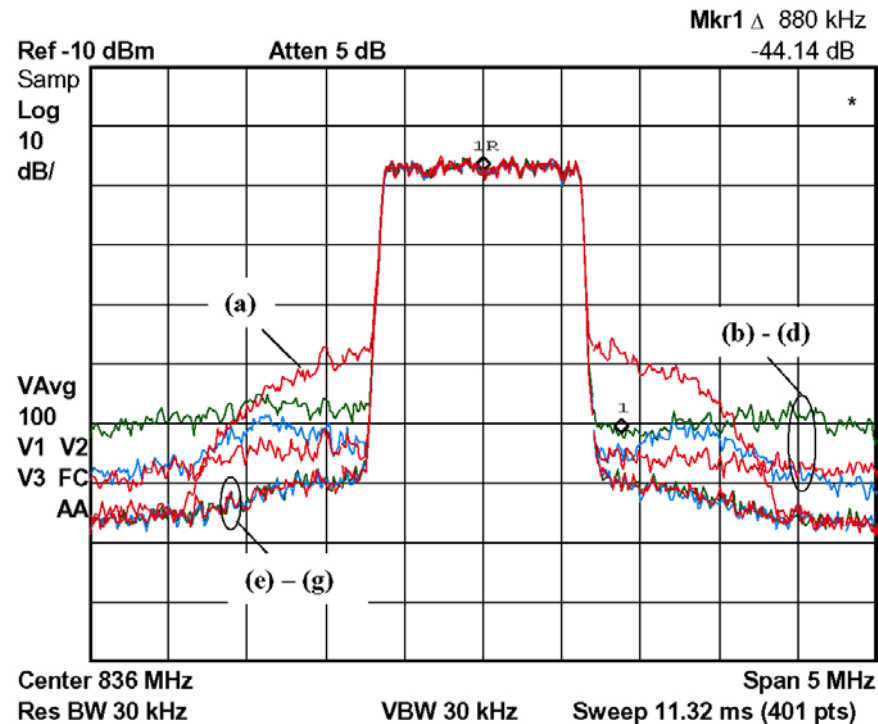


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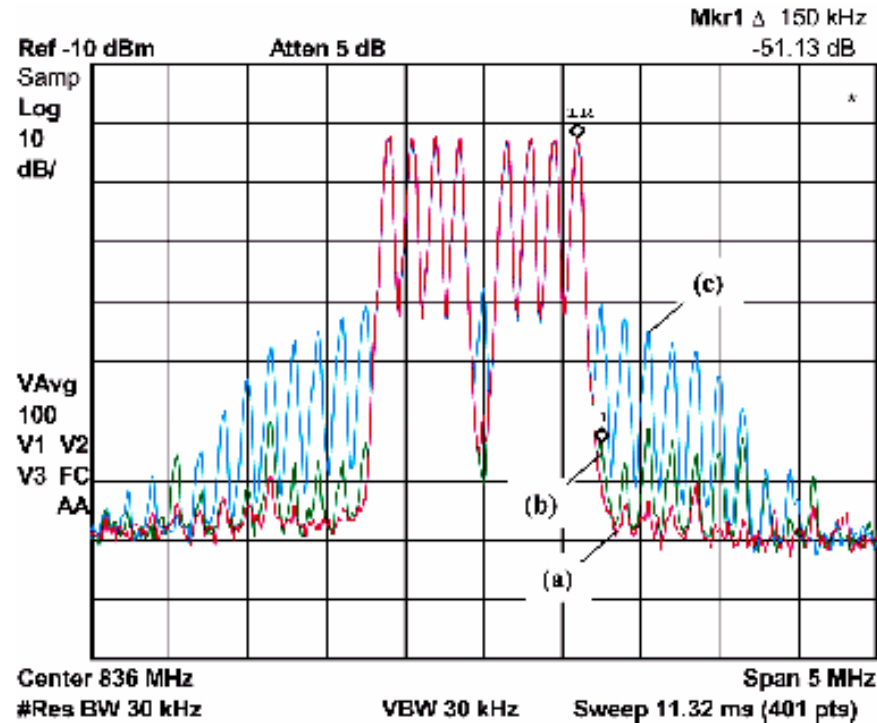
# Conventional vs. Orthogonal Polynomials



- Siemens 1 W bandset PA. Input: 1.25 MHz bandwidth OFDM signal.
- Measured PA output power spectral densities (PSDs): (a) without predistortion; (b)-(d) with conventional memory polynomial predistortion at iteration numbers 3, 4, and 5; (e)-(g) with orthogonal memory polynomial predistortion at iteration numbers 3, 4, and 5. Both the conventional and the orthogonal polynomial predistorters used  $K = 5$  and  $Q = 4$ .

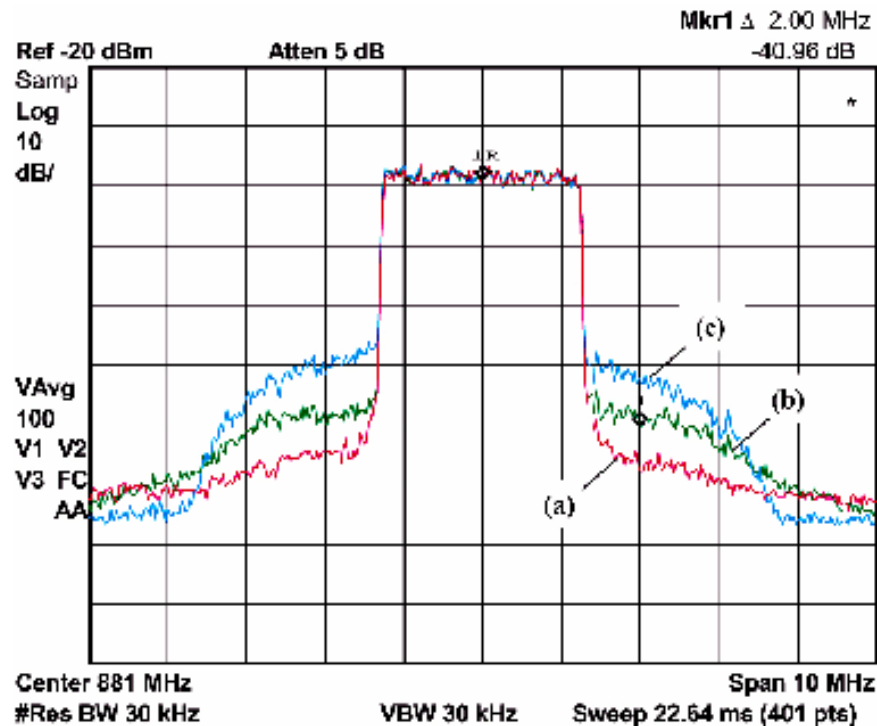


# Memoryless vs. Memory Polynomials



- Siemens 1 W handset PA. Input: 1.2 MHz bandwidth 8-tone signal.
- Measured PA output PSDs: (a) with  $K=5$ ,  $Q=9$  memory polynomial predistorter; (b) with  $K=5$  memoryless predistorter; (c) without predistortion.

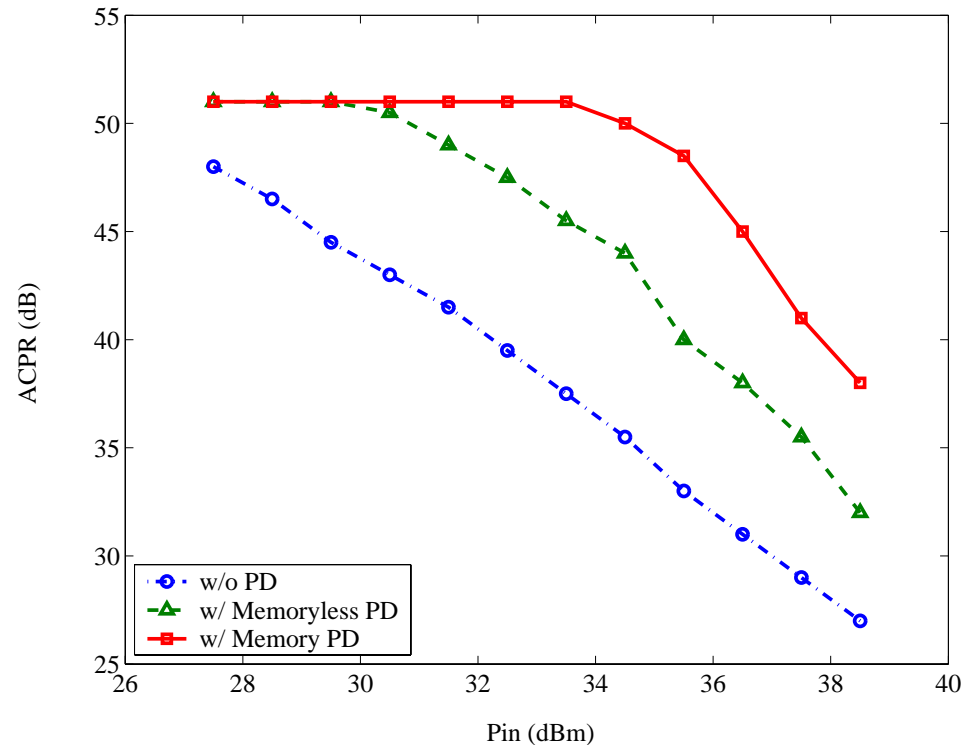
# Memoryless vs. Memory Polynomials (Cont'd)



- Ericsson 45 W base station PA. Input: 2.5 MHz bandwidth OFDM signal.
- Measured PA output PSDs: (a) with  $K=5$ ,  $Q=4$  memory polynomial predistorter; (b) with  $K=5$  memoryless predistorter; (c) without predistortion.



# Efficiency Enhancement



- ACPR = adjacent channel power ratio.
- For memoryless polynomial model  $K=5$ ; for memory polynomial model  $K=5$ ,  $Q=4$ .
- If the spectral mask requires the ACPR to be 45 dB, an average power gain of 7 dB is achieved when the memory polynomial predistorter is applied.



# Conclusions

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- A wireless test-bed for digital baseband predistortion linearization is developed.
- Orthogonal polynomials have better numerical stability than conventional ones.
- Memory polynomial predistorter is robust and has good linearization performance for PAs with memory effects.

